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# Morphological Analyses using 3D Building Databases:

## Phoenix, Arizona

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#### **Abstract**

This report summarizes our calculations of building morphological characteristics for a 16.7-km² area centered around the downtown of Phoenix, Arizona. A three-dimensional building dataset, digital orthophotos, detailed land use/cover information, bald-earth topography, and roads were integrated and analyzed using a geographic information system (GIS). Building height characteristics (e.g., mean height, variance of height, height histograms) were determined for the entire study area and broken down by land use type using a dataset that contained 7,997 buildings. Other parameters describing the urban morphology that were calculated include the building plan area fraction ( $\square_p$ ), building area density ( $a_P(z)$ ), rooftop area density ( $a_r(z)$ ), frontal area index ( $\square_p$ ), frontal area density ( $a_F(z)$ ), complete aspect ratio ( $\square_p$ ), building surface area to plan area ratio ( $\square_p$ ), and the height-to-width ratio ( $\square_p$ ). Aerodynamic roughness length ( $z_0$ ) and zero-plane displacement height ( $z_d$ ) were calculated for the entire study area and for each land use type using standard morphometric equations and the computed urban morphological parameters.

The urban morphological parameters were computed as a function of land use type, on spatial grids, and in some cases as a function of height above ground elevation. Building statistics were correlated to underlying land use using two different land use classification schemes: the seven USGS Anderson Level 2 urban land use types and a second scheme containing more detailed residential and commercial categories. Most of the morphometric parameters that we calculated were found to be similar to values computed for other cities by other researchers. The results indicate that the calculated urban morphological parameters are significantly different between different land use types. Significant differences were also noted between subcategories of residential land Moreover, commercial areas were found to have very different morphological characteristics as compared to other urban land use types, primarily because commercial areas have pockets of densely packed tall buildings. The findings presented herein are intended to be utilized in urban canopy parameterizations found in mesoscale meteorological and urban dispersions models.

#### 1.0 Introduction

Describing the urban terrain and land use/land cover (LULC) characteristics accurately is vital for urban planning, environmental management, environmental modeling, and many other applications. Urban terrain elements can be broadly classified as natural landscape, ornamental vegetation, bare soil or rock, buildings, impervious surfaces, driveways, sidewalks, or other infrastructure. Comprehensive urban databases containing urban terrain and LULC information are essential inputs for numerous meteorological modeling applications, e.g., simulating the atmospheric flow over cities, quantifying energy fluxes radiated to and from urban surfaces, determining the fate and transport of atmospheric contaminants in built-up areas. The minimum datasets required to describe the urban terrain in three dimensions include bald-earth digital elevation model (DEM), tree canopy and vegetative cover, land use/land cover, infrastructure, and building footprint outlines with height attribute.

The motivation for this research is the need to efficiently compute building morphological parameters for mesoscale meteorological modeling and air quality applications (see Ratti et al. 2001 and Brown 1999). The research objectives are to collect detailed urban datasets in a geographic information system (GIS) environment, develop automated procedures to calculate building morphological parameters, and integrate these urban canopy parameter values with detailed LULC datasets to derive relationships between the parameters and urban land use type. This report describes our efforts for a 16.7-km² section centered on the downtown of Phoenix, Arizona. In the next section of this report a brief accounting of prior efforts in this area is given, followed by a description of the accumulated datasets in the Phoenix GIS database in Section 3.0. In Section 4.0, we include an overview of how the building morphological parameters are used in the models, a short description of the calculation procedures for deriving the morphological parameters, and then present the calculation results. The report ends with a summary in Section 5.0.

#### 2.0 Background

A handful of researchers over the years have pioneered the work on obtaining building morphological statistics for cities (e.g., Ellefsen 1990, Voogt and Oke 1997, Cionco and Ellefsen 1998, Grimmond and Oke 1999). These studies have provided much useful information on building parameters, focusing mostly on residential areas and, for a few cities, industrial and commercial areas as well. There are not enough analyses, however, to make generalizations about building statistics for all U.S. cities. In addition, many of the analyses did not include the full complement of building statistics required by the CBNP suite of atmospheric transport and dispersion models. Past work involved detailed in situ studies, using visual surveys of buildings in an area encompassing a few city blocks and extrapolating the results to the entire city. With the recent availability of digital 3D building data sets, calculation of building statistics has become automated using image analysis and geographical information system (GIS) software allowing larger areas to be analyzed (e.g., Ratti et al., 2001; Burian et al., 2002a). We have recently completed data reports on building morphological statistics for downtown Los Angeles (Burian et al., 2002b) and Salt Lake City (Burian et al. 2002c), and have been working on analyses for Portland, Albuquerque, Oklahoma City, and Houston. Eastern U.S. cities will be addressed in future studies.

#### 3.0 Phoenix Urban Database

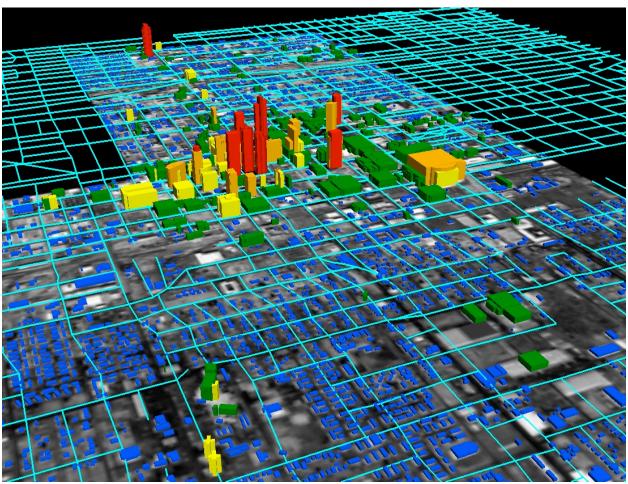
#### 3.1 Urban Morphology

Urban building, tree canopy, and DEM datasets can be purchased from commercial vendors or derived in-house. The resolution, accuracy, cost, and level of detail are important dataset characteristics to consider during the acquisition phase. The basic level of information supplied with purchased building datasets is typically the building footprint and the elevation of the rooftop. More sophisticated (and likely more expensive) datasets will have greater detail of the building (e.g., representation of rooftop structures) and include additional pieces of information (e.g., rooftop color and pitch, materials). Table 1 lists several commercial vendors that provide building, tree canopy, and DEM datasets and other digital urban data products. Digital building datasets can currently be obtained for numerous U.S. and international cities and more are rapidly becoming available. In most cases the vendor can provide the dataset in a variety of generic vector or raster data formats or data formats specific to the commercial software packages (e.g., ESRI shapefiles).

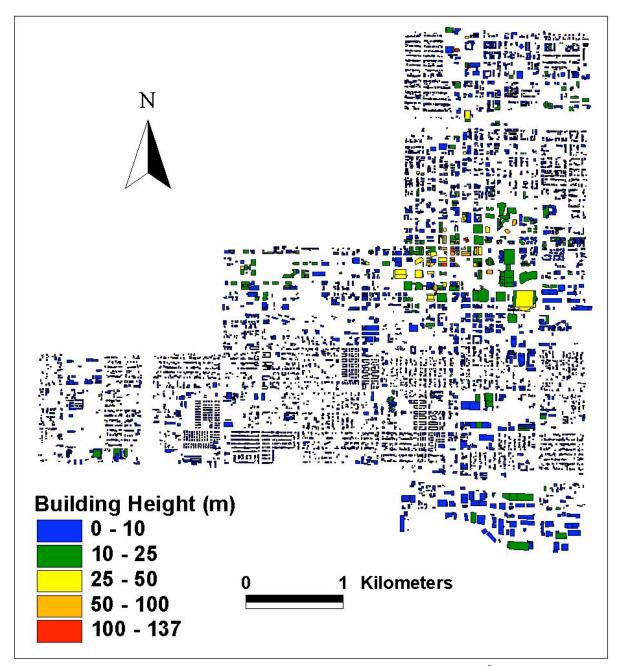
Table 1. Commercial vendors of building datasets

Vendor	Web Site
i-cubed	www.i3.com
Istar USA	www.istar.com
The Gemi Store	www.gemistore.com
Urban Data Solutions, Inc.	www.u-data.com
Vexcel Corporation	www.vexcel.com
Terrapoint (lidar)	www.transamerica.com/business_services/real_estate/terrapoint/default.asp

We contracted Vexcel Corporation to prepare the high-resolution building dataset of the Phoenix downtown area in ESRI ArcView shapefile format. The GIS shapefile-format building data are in the form of 2D polygons with height above ground as an attribute. The absolute planimetric (x,y) accuracy is 5~8 meters and vertical (z) accuracy is approximately 2 meters. The relative accuracy is between 1~3 meter Root Mean Square Error (RMSE) in xy and 1 meter RMSE for height measurements. Tree canopy data were not obtained for the study area because analysis of an aerial photograph indicated that few trees or bushes are present in downtown Phoenix. The Phoenix dataset we obtained includes 7,997 buildings in the downtown region and adjacent areas of predominantly residential, industrial, and commercial land uses (see Figures 1 and 2).



**Figure 1.** 3-D view from the southwest of the Phoenix building database. The domain covers a polygonal area 5-km by 6-km at its largest dimensions. Buildings are color coded by height (see Figure 2) and are overlaid onto a street map and digital orthophoto.



**Figure 2.** Plan view of the Phoenix building database. The domain covers 16.7 km<sup>2</sup>. Buildings are color-coded by height.

#### 3.2 Urban Land Use/Land Cover (LULC)

A major objective of this research project is to derive relationships between building morphological parameters and urban land use type. To meet this objective we need to spatially relate building morphological parameters with a manageable number of urban land use types. LULC data for areas in the United States can be obtained from several sources including federal agencies (e.g., U.S. Geological Survey (USGS), U.S. Environmental Protection Agency (USEPA)), state agencies, local/regional planning agencies, universities, researchers, commercial

vendors, and others. In general, datasets obtained from the federal, state, local/regional planning agencies, universities, or other researchers are free or cost a nominal fee. Commercial vendors on the other hand will provide a specific product with additional quality control for a greater price.

The land use dataset selected for the Phoenix area was obtained from the Maricopa Association of Governments (MAG). The MAG dataset has a minimum polygon size of 0.25 ha (2500 m<sup>2</sup>) and is based on low-altitude aerial photographs collected during 1995. The MAG dataset is classified into 26 land use types, 24 of which are urban (see Appendix 1). The MAG dataset was aggregated into two urban land use classification schemes: the first corresponding to the USGS Anderson Level 2 categories and the second with more detailed classification of the Residential, Commercial & Services, and Other Urban or Built-up land use categories. This land use classification is consistent with previous building morphological work completed for Los Angeles (Burian et al. 2002b) and Salt Lake City (Burian et al. 2002c). Table 2 summarizes the land use types in each classification scheme and Appendix 2 provides further descriptions of the land use categories. The seven categories for the first scheme are (1) Residential, (2) Commercial & Services, (3) Industrial, (4) Transportation/Communications/Utilities, (5) Mixed Industrial & Commercial, (6) Mixed Urban or Built-up, and (7) Other Urban or Built-up. This is the same scheme used to classify urban land use in the USGS/EPA GIRAS national LULC dataset. The second classification scheme contains subcategories for Residential, Commercial & Services, and Other Urban or Built-up land use types. The Residential category is divided into four subcategories: (1) Low-density Single-family, (2) High-density Single-family, (3) Multifamily, and (4) Mixed. Building density and vegetation characteristics are expected to be significantly different between the four types of residential land use. The Commercial & Services category has been divided into two subcategories (Non-high-rise and High-rise) in previous research efforts, but was not possible for Phoenix because the MAG data did not identify high-rise land uses. The Other Urban or Built-up category is also divided into two subcategories: Predominantly Vegetated and Predominantly Built-up.

Another land use category called Urban High-rise has been defined in previous research efforts, but was not defined for Phoenix because the MAG dataset did not include enough information to identify Urban High-rise areas. However, we were able to delineate a Downtown Core Area to include the city center based on our collective knowledge of the city, site visits, and the digital orthophoto. The Downtown Core Area will overlap with the land uses in our two classification schemes, but it is needed so we can analyze and better define the characteristics of the city center area of Phoenix.

Our land use data indicates that the 16.7-km<sup>2</sup> study area is a highly urbanized region of Phoenix consisting of a part of the downtown region (containing high-rise buildings), as well as High-density Single-family Residential and Industrial areas. The land use distribution listed in Table 2 suggests that most of the land use is Commercial & Services, Residential, and Industrial with a small fraction of Transportation and Other Urban or Built-up. This land use distribution is similar to other cities we have analyzed (e.g., Burian et al. 2002b).

Note that the study area does not include Low-density Single-Family Residential or Mixed Residential land uses. The MAG dataset includes a low-density residential land use class, but it

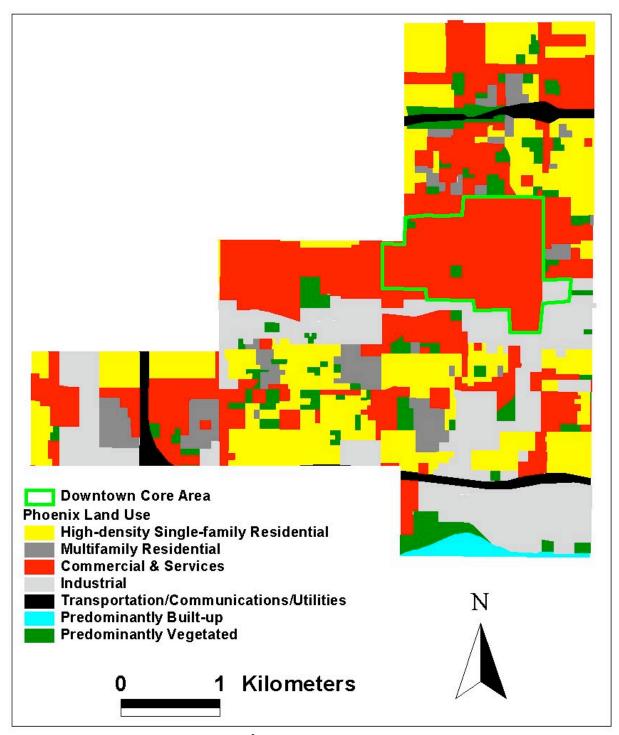
is not present in the study area. But, the MAG dataset does not include a Mixed Residential land use class, which was an initial concern. A review of the digital orthophoto suggested the MAG dataset adequately sub-divided the Residential into single family and multifamily. Therefore, we were satisfied with the classification set forth in MAG and did not modify the dataset.

Figure 3 shows our derived LULC dataset for the 16.7-km<sup>2</sup> study area in Phoenix after aggregation to the 12-category land use scheme. Also shown is the boundary of the Downtown Core Area. The LULC dataset was intersected with the building dataset using the ESRI ArcView GIS software to identify which buildings were associated with which land use type. Fortran codes and Avenue scripts previously written, as well as standard ArcView GIS functions, were used to calculate a suite of urban morphological parameters. The calculation procedures and the results of the analyses are described next in Section 4.

Table 2. Urban land use coverage in the 16.7-km<sup>2</sup> study area

Land Use Class	Area (ha)*	Percent of Total (%)
Residential	514	31
Low-density Single-family (< 8 units/hectare)	0	0
High-density Single-family (≥ 8 units/hectare)	414	25
Multifamily	100	6
Mixed	0	0
Commercial & Services	620	37
Non-high-rise		
High-rise		
Industrial	348	21
Transportation/Communications/Utilities	51	3
Mixed Industrial & Commercial	0	0
Mixed Urban or Built-up	0	0
Other Urban or Built-up	139	8
Predominantly Vegetated	120	7
Predominantly Built-up	20	1
Urban High-rise		
Downtown Core Area	162	10

<sup>\*</sup> The areas are given in hectares (ha) (100 ha =  $1 \text{ km}^2$ ).



**Figure 3.** LULC dataset for the 16.7-km<sup>2</sup> study area aggregated to 12-category building analysis land use classification scheme.

#### 4.0 Derivation of Urban Morphological Parameters

In the next ten sub-sections, we calculate building morphological parameters that are used in atmospheric models and dispersion models to account for urban effects. These calculations include building height statistics, the building plan area fraction  $(\Box_p)$ , building area density  $(a_P(z))$ , rooftop area density  $(a_r(z))$ , frontal area index  $(\Box_p)$ , frontal area density  $(a_F(z))$ , complete aspect ratio  $(\Box_C)$ , building surface area to plan area ratio  $(\Box_B)$ , height-to-width ratio  $(\Box_S)$ , the roughness length  $(z_o)$ , and the displacement height  $(z_d)$ . The calculation procedures and results are summarized in each sub-section.

#### 4.1 Building Height Characteristics

Background. In this sub-section we summarize the height characteristics of buildings in the 16.7-km<sup>2</sup> study area. Average building height yields information on the depth through which the urban canopy directly impacts the atmosphere. Average building height (multiplied by a proportionality constant) can be used as a first-order approximation of the surface roughness  $z_0$  (see Section 4.10). Surface roughness is used in air quality and meteorological models to account for enhanced mixing and the drag effects of the underlying surface. Canopy height is often used as the length scale in the canopy layer. Urban field experiment data evaluations have suggested that similarity theory is valid somewhere above the canopy height. Below canopy height, drag parameterizations can be used to account for reduced air flow due to the urban fabric. Variation in canopy height may prove to be important in parameterizations of turbulence production.

*Calculation Methods.* The mean and standard deviation of building height were calculated using the following equations:

$$\overline{h} = \frac{\prod_{i=1}^{N} h_i}{N} \tag{1}$$

$$S_h = \sqrt{\frac{\prod_{i=1}^{N} \left( h_i \square \overline{h} \right)}{N \square 1}}$$
 (2)

where  $\overline{h}$  is the mean building height,  $s_h$  is the standard deviation of building height,  $h_i$  is the height of building i, and N is the total number of buildings in the area. The average building height weighted by building plan area was calculated using the following equation:

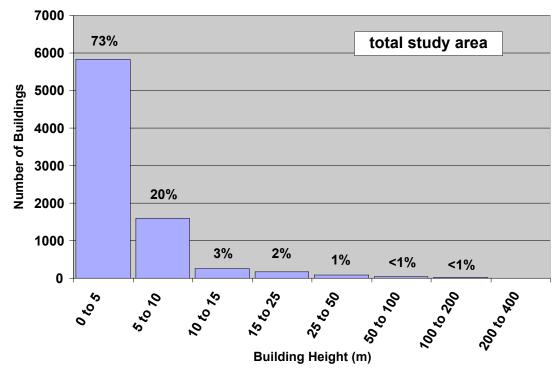
$$\overline{h}_{AW} = \frac{\prod_{i=1}^{N} A_i h_i}{\prod_{i=1}^{N} A_i}$$
(3)

where  $\overline{h}_{AW}$  is the mean building height weighted by building plan area, and  $A_i$  is the plan area at ground level of building i.

Results. For the 16.7-km<sup>2</sup> study area, the mean building height based on Eqn. (1) was calculated to be 5.6 m and the standard deviation was calculated to be 7.6 m. The mean building height weighted by plan area was computed to be 9.2 m for the study area, indicating that taller buildings have greater plan area on average. The building heights in the study area range from 3 m to 137 m.

Figure 4 is a histogram of building heights for the study area. Note that the building height bin widths are not equal and grow in size with height. The distribution is unimodal, with nearly 93% of the buildings being between 0 and 10 m high. There are only 11 buildings with heights greater than 100 meters. The high amount of shorter buildings can be explained by the high amount of residential structures included in the study area.

Figures 5, 6, 7, and 8 show the building height histograms for four of the land uses in the 7-category land use scheme: Residential, Commercial & Services, Industrial, and Other Urban or Built-up. Figures 5 and 7 show that Residential and Industrial buildings are predominantly two or three story structures, with a few high-rise apartment buildings present in the residential area. In the Commercial & Services land use category (Fig. 6) we observe a similar distribution of building heights, but with a higher frequency of buildings with heights greater than 25 meters, which is expected because it includes the downtown area with high rises. The building height distributions for the Residential (Fig. 5), Industrial (Fig. 7), and Other Urban or Built-up (Fig. 8) land use types have similar building height distributions with a 0-5 m mode and greater than 90% of the buildings between 0 and 10 m tall.



**Figure 4.** Distribution of building heights in the 16.7-km<sup>2</sup> downtown Phoenix study area. The percent of buildings in each height category are shown above each bar in the chart.

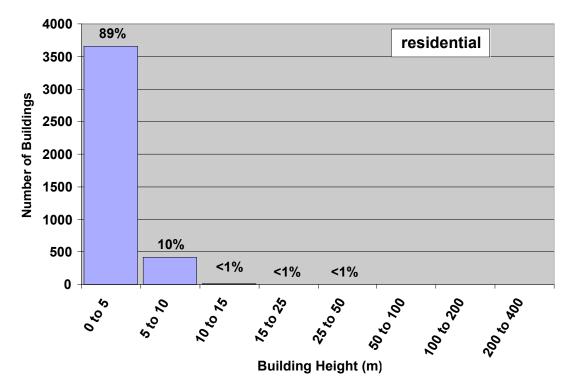


Figure 5. Distribution of building heights in the residential land use category.

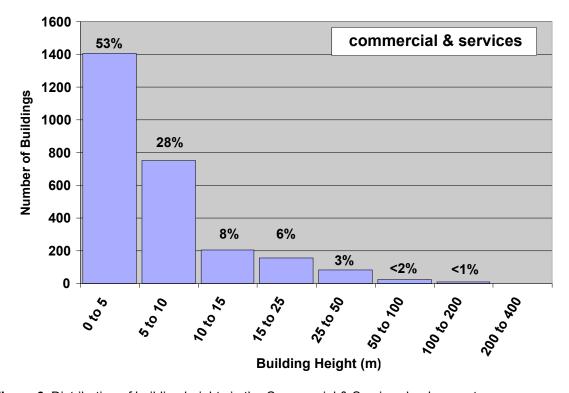


Figure 6. Distribution of building heights in the Commercial & Services land use category.

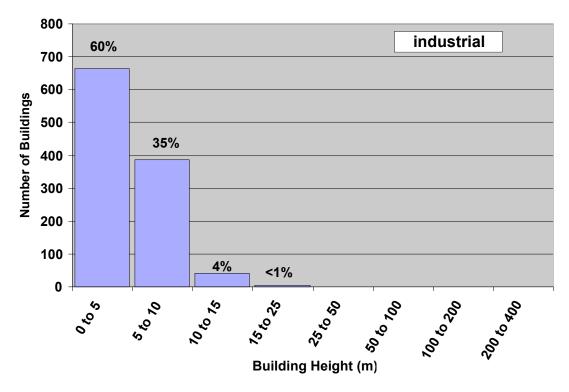


Figure 7. Distribution of building heights in the Industrial land use category.

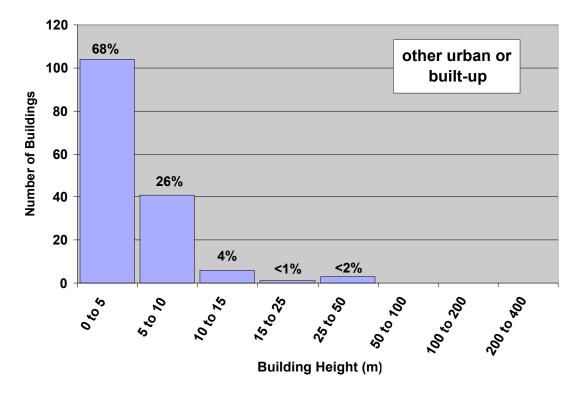


Figure 8. Distribution of building heights in the Other Urban or Built-up land use category.

Figures 9 and 10 show the building height distributions for the High-density Single-family Residential and the Multifamily Residential land use categories (recall that Low-density Single-family Residential and Mixed Residential land uses are not found in the study area). The High-density Single-family Residential building height distribution is dominated by single story structures (the 0-5 m height bin). The Multifamily Residential land use category contains high-rise apartment and condominium buildings; therefore, the building height distribution contains a higher frequency of buildings in the 10-15 and 15-25 meter height bins than the High-density Single-family Residential.

Figure 11 shows the building height histogram for the Downtown Core Area. The Downtown Core Area is defined as the concentrated area of high-rise structures in the downtown area of a city, which is verified by the building height distribution shown in Figure 11. A bimodal distribution is apparent with one mode at the 5-10 m height bin and the second at the 15-25 m height bin.

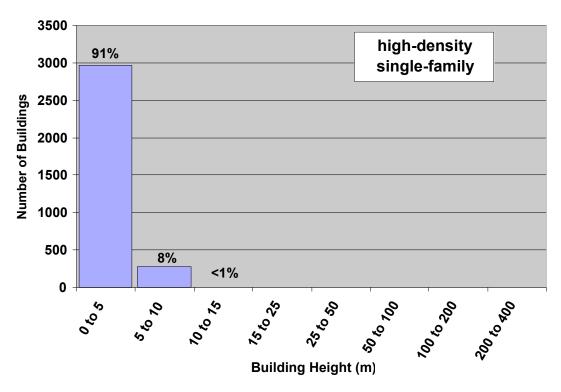


Figure 9. Distribution of building heights in the High-density Single-family Residential land use category.

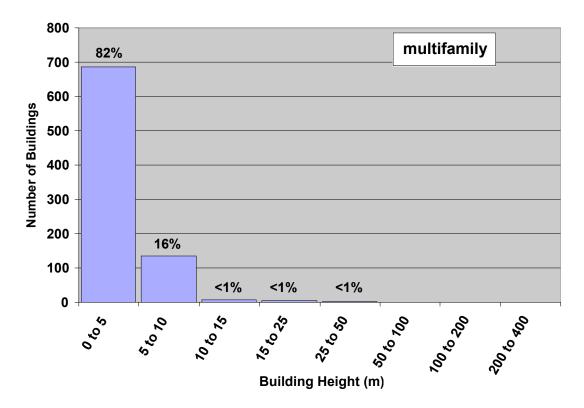


Figure 10. Distribution of building heights in the Multifamily Residential land use category.

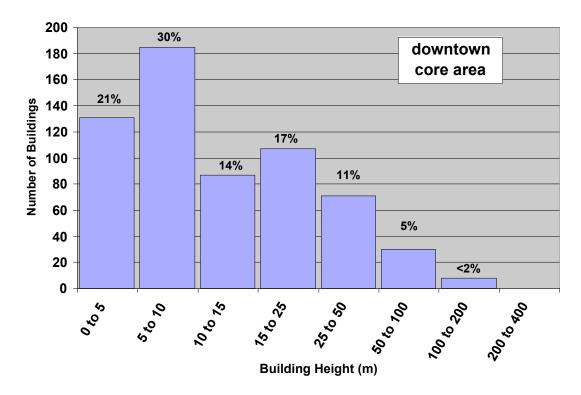
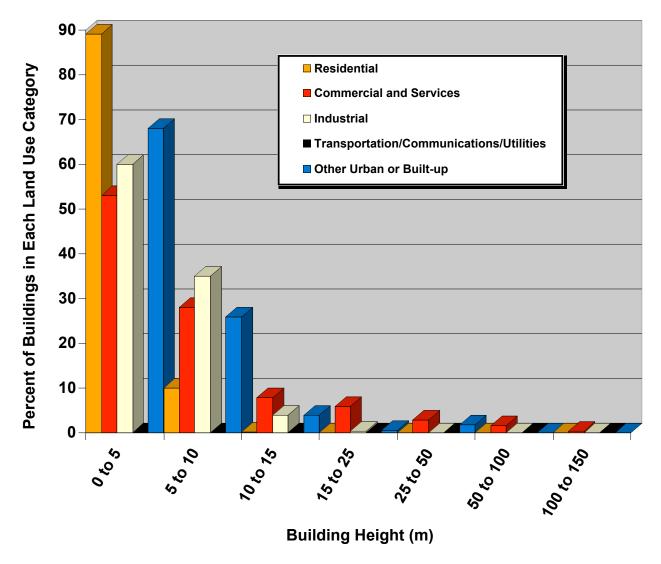
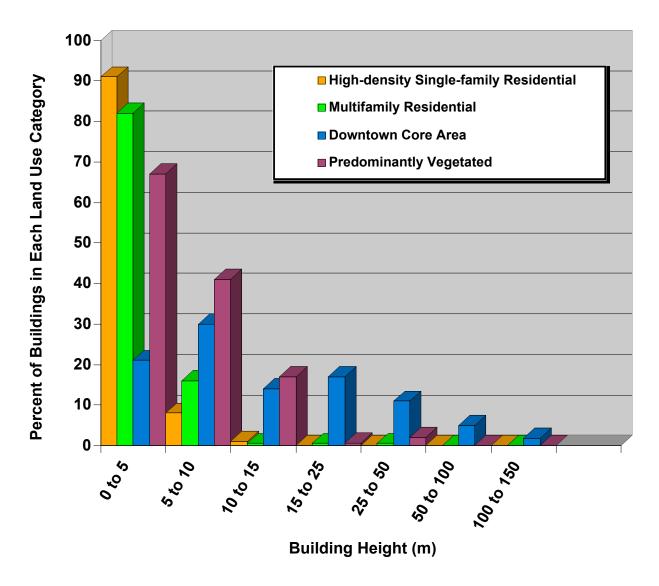


Figure 11. Distribution of building heights in the Downtown Core Area land use category.

Figure 12 displays a comparison of building height histograms in percentage form for all land use types in the 7-category classification scheme all in the same plot. Figure 13 shows the height histogram comparison for the 12-category land use scheme (the plot only includes those land use present and containing a significant number of buildings) and the Downtown Core Area. One can better see in these plots the similarities and differences between different land use categories. Recall, however, that some of the land uses have significantly more buildings than others.



**Figure 12.** Comparison of the percent of buildings in each height increment for each 7-category land use type.



**Figure 13.** Comparison of the percent of buildings in each height increment for Residential and Commercial & Services sub-categories and the special High-rise land use types.

Table 3 summarizes the building height characteristics as a function of land use. Several interesting features stand out. The building heights in the Multifamily Residential land use have a higher standard deviation than the building heights in the High-density Single-family Residential land use. This observation indicates the greater range of building heights (including taller apartment buildings) in the Multifamily Residential category. Table 3 also shows that the Industrial land use type is predominantly made up of shorter buildings (note the mean height of 5.1 m and the small standard deviation of 2.2 m), while Commercial & Services land use contains the taller buildings (mean height of 8.5 m and standard deviation of 12.4 m). The high standard deviation in the Commercial & Services category indicates once again a wide range of building heights in the category. The buildings in the Downtown Core Area have an average

height of 17.2 m, and a standard deviation of 20.7 m. The high-rise sections of Phoenix have relatively short buildings for a major U.S. city, comparable to Salt Lake City. For comparison, the average building height in the Downtown Core Area of Los Angeles is 45.0 m.

**Table 3.** Summary of building characteristics for the downtown Phoenix study area as a function of land use type.

Finderlix study area as a function of failuruse type.					
Land Use Class	Number of Buildings	Average Height (m)	Standard Deviation	Plan Area- weighted Average Height (m)	
Residential	4083	3.8	1.5	4.2	
Low-density Single-family (< 8					
units/hectare) High-density Single-family (≥ 8	3248	3.7	1.0	3.9	
units/hectare) Multifamily	836	4.2	2.7	4.7	
Mixed					
Commercial & Services	2656	8.5	12.4	13.1	
Non-high-rise					
High-rise					
Industrial	1103	5.1	2.2	7.1	
Transportation/Communications/Utilities	0	0	0	0	
Mixed Industrial & Commercial					
Mixed Urban or Built-up					
Other Urban or Built-up	155	5.4	4.1	8.3	
Predominantly Vegetated	155	5.4	4.1	8.3	
Predominantly Built-up	0	0	0	0	
Urban High-rise					
Downtown Core Area	619	17.2	20.7	21.2	

#### 4.2 Building Plan Area Fraction ( )

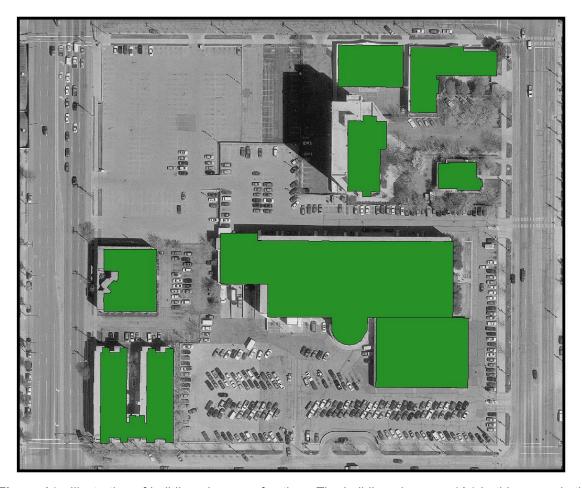
Background. Building plan area fraction has been shown to be related to the surface roughness  $z_0$  (see Section 4.10). Surface roughness is used in air quality and meteorological models to account for enhanced mixing and drag effects of the rough surface. In the urban context, as the density of buildings (plan area fraction) increases so does the roughness of the system, but a threshold is eventually reached where adding new elements effectively reduces the drag of the elements present (Grimmond and Oke 1999). The density of buildings also indicates the potential flow regime. Hussain and Lee (1980) performed wind-tunnel experiments and found that three flow regimes develop in idealized urban street canyons: (1) isolated flow, (2) wake interference flow, and (3) skimming flow. The isolated flow regime occurs when elements are spaced relatively far apart ( $0 < D_p < 0.1$ ), the wake interference flow occurs when elements are spaced at a medium density level ( $0.1 < D_p < 0.6$ ), and the skimming flow regime occurs for high-density building arrangements ( $D_p > 0.6$ ) (Oke 1988).

Calculation Methods. The building plan area fraction ( $\square_p$ ) is defined as the ratio of the plan area of buildings to the total surface area of the study region:

$$\Box_p = \frac{A_p}{A_T} \tag{4}$$

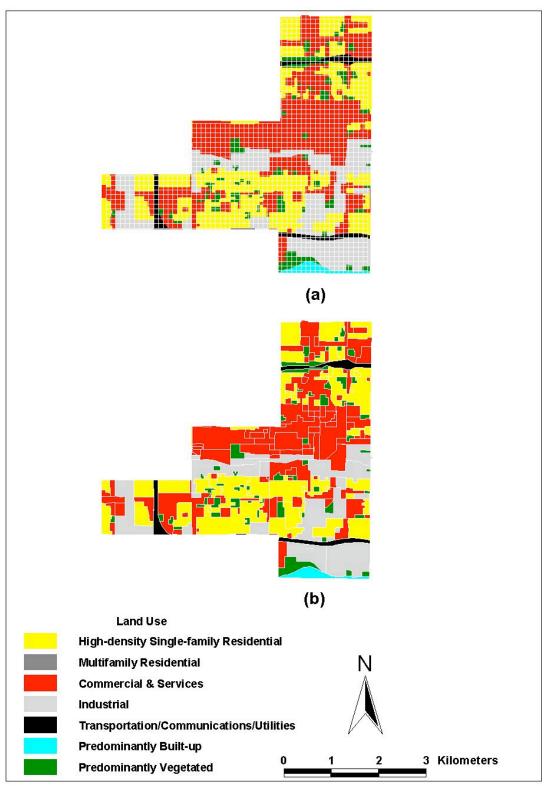
where  $A_p$  is the plan area of buildings at ground level, i.e., the footprint area, and  $A_T$  is the total plan area of the region of interest, i.e., an arbitrary area that encompasses the buildings (see Figure 14). The computed value of the plan area fraction is dependent on the size of the area or the specific land use types included in the calculation. In most cases the plan area fraction will vary significantly from one city block to the next because of the heterogeneous nature of the urban landscape. The appropriate size of the calculation element should be chosen such that the characteristics of interest in the urban area are homogeneous and discernible.

Results. For the 16.7-km<sup>2</sup> study area the plan area fraction at ground level was calculated to be 0.16. This value is significantly lower than the plan area fraction of 0.47 found for Mexico City, Mexico (Grimmond and Oke 1999) and the 0.37 found for Vancouver, British Columbia, Canada (Voogt and Oke 1997), but more consistent with the 0.23 found for Salt Lake City (Burian et al. 2002c). The difference is partially due to the newer development patterns with relatively wide streets and greater amounts of open space in downtown Phoenix compared to the downtown areas of the Mexico City and Vancouver. Another reason is the study area for Phoenix is much greater in aerial extent than the Mexico City and Vancouver sites and includes a higher amount of residential areas, which usually have lower building plan area fractions than commercial and industrial areas.

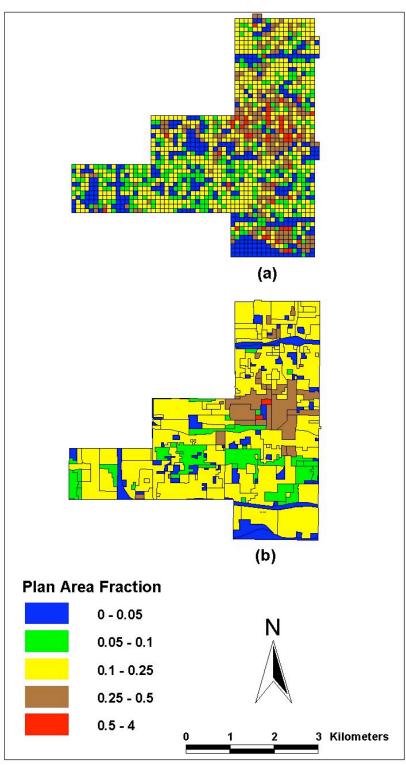


**Figure 14.** Illustration of building plan area fraction. The building plan area  $(A_p)$  in this scene is the sum of the areas of the building footprints shown in green. The total plan area  $(A_T)$  is the area enclosed by the outline of the figure. The building plan area fraction  $(\Box_p)$  is computed by dividing building plan area  $(A_p)$  by total plan area  $(A_T)$ .

We have calculated the plan area fraction on two meshes overlaid onto the study area in order to view the spatial heterogeneity. Figure 15 shows the two meshes overlaid onto land use: in the first case, a uniform 100-m X 100-m rectilinear grid cell mesh covering the entire 16.7-km² study area, and in the second case a non-uniform polygonal grid cell mesh based on the street network and land use. Figure 16 shows the plan area fraction according to the two grid cell meshes. It is clear by comparison that there is significant variation within the polygonal meshes that follow the street network. The major highways and the dry bed of the Salt River running through the study area are clearly visible on the uniform mesh as open areas (low values of  $\square_p$ ). It is more difficult to see a one-to-one correlation with urban land use type, i.e., there appears to be significant variation in  $\square_p$  within an urban land use type. For example, in the industrial area in the south end of the study area (gray region, Fig. 15), the plan area fraction ranges from high density to relatively open areas (Fig. 16).



**Figure 15.** Grid cells used to display and analyze the spatial heterogeneity of the Phoenix building morphology for the 16.7-km<sup>2</sup> study area. Urban land use type overlaid with (a) the 100m X 100m uniform grid cell mesh, and (b) the non-uniform grid cells based on street network.



**Figure 16.** Spatial variability of building plan area fraction ( $\square_p$ ) distributed according to a uniform 100-m X 100-m grid mesh and a non-uniform grid mesh based on the downtown road network.

Table 4 contains the computed  $\square_p$  for each land use type in the land use classification schemes described in Section 3.2. Table 4 indicates that the Commercial & Services and the Industrial land use categories have a significantly higher density than the Residential land use types. The Other Urban or Built-up land use contains only a few buildings and hence has a low plan area fraction. Most of the average values shown in Table 4 fall within the  $\square_p$  range for wake interference flow  $(0.1 < \square_p < 0.6)$  (Hussain and Lee 1980).

**Table 4.** Plan area fraction as a function of land use type

Land Use Class	$\bigcap_{\mathcal{D}}$
Residential	0.13
Low-density Single-family (< 8 units/hectare)	
High-density Single-family (≥ 8 units/hectare)	0.11
Multifamily	0.18
Mixed	
Commercial & Services	0.20
Non-high-rise	
High-rise	
Industrial	0.19
Transportation/Communications/Utilities	0.00
Mixed Industrial & Commercial	
Mixed Urban or Built-up	
Other Urban or Built-up	0.04
Predominantly Vegetated	0.04
Predominantly Built-up	
Urban High-rise	
Downtown Core Area	0.32

In Table 5, we compare the computed plan area fraction values for several land use types in Phoenix to those reported in other studies. Our computed values of  $\square_p$  for Residential and Industrial land use types are smaller than those of other cities. The plan area fraction values computed in these other studies have included the plan area of trees in residential areas, which can be a significant fraction of the plan area. Trees are not included in our calculations of  $\square_p$  and explain some of the differences. However, visual inspection of aerial photos suggests that there are relatively few trees and shrubs in the high-density residential areas in our study region. The relatively low values for the Phoenix downtown area can also be attributed to the mor emodern development patterns in the U.S., which incorporate greater open space and wider streets.

**Table 5.** Comparison of plan area fraction ( $\square_p$ ) for downtown Phoenix to other cities. Locations grouped by land use type and then listed in order of decreasing  $\square_p$ .

Location	Land Use Class	Др	Source
Vancouver, BC, Canada	Suburban residential	0.62	Voogt and Oke (1997)
Sacramento, CA	Suburban residential	0.58	Grimmond and Oke (1999)
Arcadia, CA	Suburban residential	0.53	Grimmond and Oke (1999)
Chicago, IL	Suburban residential #1	0.47	Grimmond and Oke (1999)
Chicago, IL	Suburban residential #2	0.38	Grimmond and Oke (1999)
San Gabriel, CA	Suburban residential	0.36	Grimmond and Oke (1999)
Miami, FL	Suburban residential	0.35	Grimmond and Oke (1999)
Tucson, AZ	Suburban residential	0.33	Grimmond and Oke (1999)
Los Angeles, CA	Mixed residential	0.29	Burian et al. (2002b)
Los Angeles, CA	High-density single-family residential	0.27	Burian et al. (2002b)
Salt Lake City, UT	High-density single-family residential	0.19	Burian et al. (2002c)
Phoenix, AZ	Multifamily residential	0.18	This Report
Los Angeles, CA	Industrial	0.38	Burian et al. (2002b)
Vancouver, BC, Canada	Light industrial	0.38	Voogt and Oke (1997)
Salt Lake City, UT	Industrial	0.27	Burian et al. (2002c)
Phoenix, AZ	Industrial	0.19	This Report
Mexico City, Mexico	Downtown	0.47	Grimmond and Oke (1999)
Vancouver, BC, Canada	Downtown	0.37	Voogt and Oke (1997)
Salt Lake City, UT	Downtown core area 0.33		Burian et al. (2002c)
Los Angeles, CA	Urban high-rise	0.32	Burian et al. (2002b)
Phoenix, AZ	Downtown core area	0.32	This Report
Los Angeles, CA	Downtown core area	0.29	Burian et al. (2002b)

#### 4.3 Building Plan Area Density $(a_P(z))$

Background. The building plan area density gives information on how much of the air volume is occupied by buildings (when multiplied by the height increment of the volume of interest). The change in building plan area density with height yields the roof fraction (see Section 4.4). The roof fraction is important from a thermodynamic perspective because of the significant solar gain and heat loss at the building roof level. The building plan area density can be used to derive the roof area density, which is analogous to the leaf area density. The leaf area density gives information on how much long- and short-wave radiation travels through the canopy and how much is intercepted. Something similar might be done for urban areas with buildings using the building plan area density. Building plan area density can also be used as a surrogate for frontal area density (see Section 4.5) in evaluating the drag force as a function of height due to buildings in urban areas.

Calculation Methods. The building plan area density  $(a_P(z))$  is defined as the average building plan area within a height increment divided by the volume of the height increment:

$$a_{p}(z) = \frac{\frac{1}{\Box z} \prod_{z = \frac{1}{2} \Box z}^{z + \frac{1}{2} \Box z} A_{p}(z) dz}{A_{T} \Box z}$$

$$(5)$$

where,  $A_p(z')$  is the plan area of buildings at height z',  $A_T$  is the plan area of the site, and  $\Box z$  is the height increment for the calculation. Since  $A_T$  is not a function of height we can bring it into the integral in the numerator and obtain:

$$a_{p}(z) = \frac{1}{\square z} \prod_{z = \frac{1}{2}\square z}^{z + \frac{1}{2}\square z} \frac{A_{p}(z)}{A_{T}} dz \square$$

$$\square z = \frac{1}{\square z} \prod_{z = \frac{1}{2}\square z} \frac{A_{p}(z)}{A_{T}} dz \square$$
(6)

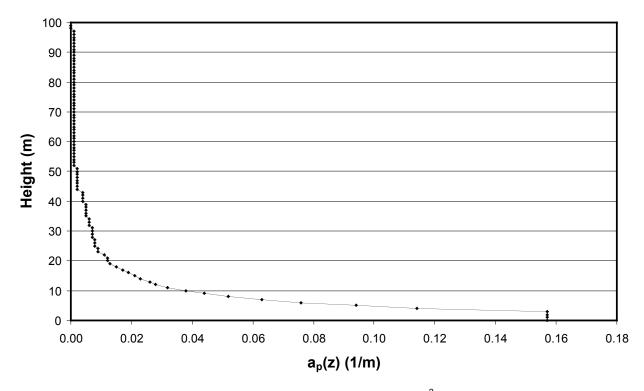
Knowing  $\square_P(z') = A_P(z')/A_T$  and assuming that the building plan area does not change appreciably within a height increment  $\square z$ , eq. (6) can be approximated by:

$$a_{p}(z) \square \frac{\square_{p}(z)}{\square z} \tag{7}$$

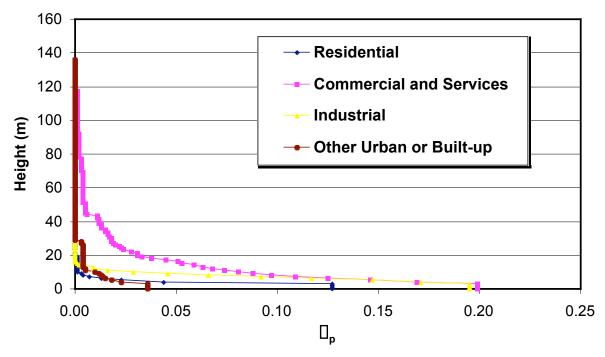
Results. Figure 17 illustrates the building plan area density function  $(a_P(z))$  for the Phoenix study area using a 1-m height increment. As expected,  $a_P(z)$  is constant for the first few meters above

ground elevation until the rooftop height of the shortest buildings are reached (approximately four meters). Building plan area density then rapidly declines with height and asymptotically approaches  $\Box_P = 0$ . Only the first 100 m above ground elevation are shown because  $a_P(z)$  is nearly zero above this height.

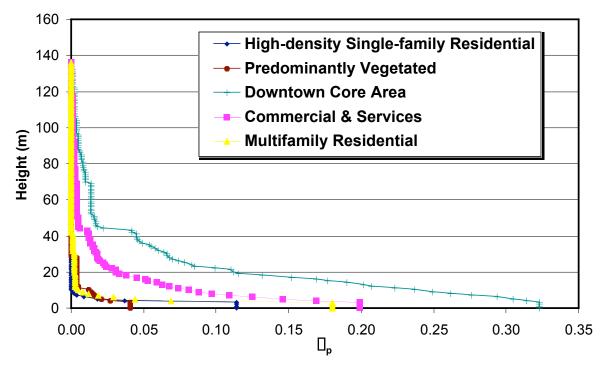
Figure 18 shows  $a_P(z)$  for the 7-category land use scheme. Only the land uses that have sufficient buildings to produce meaningful plots are illustrated. The building plan area density of the Industrial, Residential, and Other Urban or Built-up land uses decreases relatively rapidly with height above four meters, indicating that these land use categories contain mostly one, two, and three story buildings. The  $a_P(z)$  for the Commercial & Services land use is the largest near the ground, indicating that the buildings in this land use type have a large footprint and are densely packed. Figure 19 shows  $a_P(z)$  for several land use types in the 12-category scheme, as well as the Downtown Core Area. The plot shows that the  $a_P(z)$  associated with the Downtown Core Area decreases much less rapidly than the other land use types.



**Figure 17.** Building plan area density function  $(a_P(z))$  for the entire 16.7-km<sup>2</sup> downtown Phoenix area.



**Figure 18.** Building plan area density function  $(a_P(z))$  for four of the land use classes in the 7-category classification scheme.



**Figure 19.** Building plan area density function  $(a_P(z))$  for several land use types in the 12-category scheme and the Downtown Core Area.

#### 4.4 Roof Area Density $(a_r(z))$

Background. The rooftop area as a function of a height is important in describing the thermodynamics of the urban canopy. Roofs are interceptors and reflectors of solar radiation, and give off or absorb long-wave radiation. Knowledge of the roof area, therefore, is important in determining the energy balance within the urban canopy. The roof area density is a quantity that can be used to compute roof area as a function of height. The roof area density is analogous to the leaf area density. The leaf area density can be integrated from the top of the vegetative canopy to the ground to yield a leaf area index. The leaf area index gives information on how much long- and short-wave radiation travels through the canopy and how much is intercepted. Roof area density might be used in a similar fashion to help estimate energy fluxes through the urban canopy.

Calculation Methods. The rooftop area within a height increment  $\Box z$  can be approximated by the difference between the building plan areas at two heights:

$$A_r(z) = A_p \left[ z \, \Box \, \frac{\Box z}{2} \, \Box \, A_p \right] z + \frac{\Box z}{2} \, \Box$$
 (8)

where  $A_p(z)$  is the plan area of buildings at the specified height and a flat-roofed assumption has been made. The roof area density  $(a_r(z))$  can then be defined as the rooftop plan area per height increment  $\Box z$  divided by the volume of the height increment:

$$a_{r}(z) = \frac{A_{r}(z)}{A_{T} \cdot \Box z} = \frac{A_{p} + \Box z}{A_{p} + \Box z} + \frac{\Box z}{2} + \frac{\Box z}{2} + \frac{\Box z}{2}$$

$$A_{T} \cdot \Box z$$

$$(9)$$

where  $A_T$  is the total area within which buildings are contained. Analogous to the leaf area index used in the plant canopy community, the integration of  $a_r(z)$  from a specified elevation above ground (z) to the height of the canopy  $(h_c)$  is equal to the building area index (L(z)):

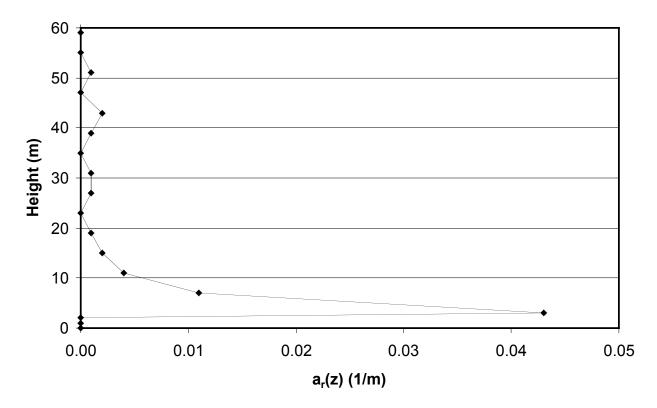
$$L(z) = \prod_{z}^{h_{c}} q_{r}(z) dz$$
 (10)

The integration of  $a_r(z)$  from ground elevation to the canopy height  $(h_c)$  is equal to  $\square_P$ :

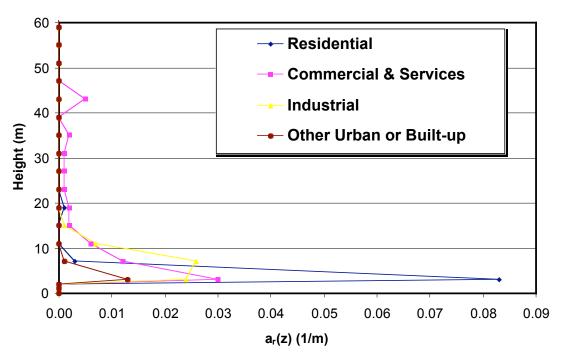
$$L(0) = \prod_{p} = \prod_{i=0}^{h_c} u_r(z) dz$$
 (11)

Results. The roof area density function  $a_r(z)$  is shown in Figure 20 for the Phoenix study area. A significant fraction of the rooftop area is located within the first 10 meters of height above ground. The value of  $a_r(z)$  is zero below 3 m because no buildings are defined to be below 3 meters (a little less than one story) in height. Figures 21 and 22 show  $a_r(z)$  for the 7-category land use scheme and for the 12-category scheme along with the Downtown Core Area, respectively. Figure 21 is limited to the first 60 meters and Figure 22 is limited to the first 100

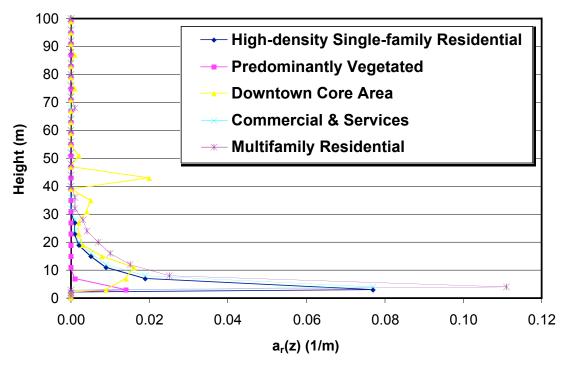
meters of height to make them more readable because for most of the land use types the first 60-100 meters of height contains all the rooftop area. The Residential and Industrial land uses consistently have the largest rooftop density fraction within 5-10 meters of the ground, whereas the Downtown Core Area has significant roof area at the 40-50 m level.



**Figure 20.** Roof area density function  $(a_r(z))$  for the Phoenix study area. Data are plotted for 1-m height increments up to 4 m and then by 4-m increments (approximately one story) up to 60 m.



**Figure 21.** Roof area density function  $(a_r(z))$  for the 7-category land use scheme. Data are plotted for 1-m height increments up to 4 m and then by 4-m increments (approximately one story) up to 60 m.



**Figure 22.** Roof area density function  $(a_r(z))$  for the classification scheme 2 land use types and the Downtown Core Area. Data are plotted for 1-m height increments up to 4 m and then by 4-m increments (approximately one story) up to 100 m.

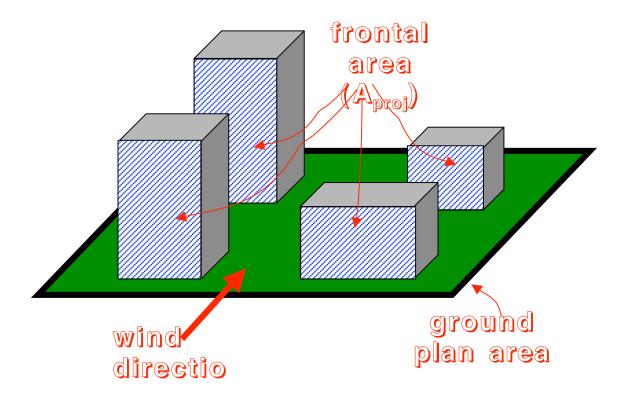
#### 4.5 Building Frontal Area Index ( ]

Background. Building walls facing into the wind impart drag on the air flow. The frontal area index, a measure of the frontal area per unit horizontal area, has been shown to be related to the surface roughness  $z_0$  (see Section 4.10). Surface roughness is used in air quality and meteorological models to account for enhanced mixing and the drag effects of the rough surface. The flow regime within urban street canyons is also thought to be a function of the frontal area index and plan area fraction (see Section 4.2).

Calculation Methods. The frontal area index ( $\square$ ) is defined as the total area of buildings projected into the plane normal to the approaching wind direction ( $A_{proj}$ ) divided by the plan area of the study site ( $A_T$ ):

$$\Box_f \left(\Box\right) = \frac{A_{proj}}{A_T} \tag{12}$$

where  $\square$  is the wind direction. Figure 23 illustrates frontal area. A script was written in Avenue (the scripting language for ArcView) during a previous research effort (Burian et al. (2002b) and modified for this analysis to automatically determine the total area of building surfaces in the projected plane normal to a specified wind direction ( $A_{proj}$ ) and calculate  $\square_f$  using Eqn. (12).



**Figure 23.** Illustration of projected frontal area. In the schematic of the four buildings shown above, the frontal area  $(A_{proj})$  is the total area of the faces exposed to the oncoming wind.

The frontal area index ( $\Box_f$ ) can be approximated from the product of mean height, breadth, and density of roughness elements (Grimmond and Oke 1999):

$$\square_f = \overline{L_y H} \square_d$$
(13)

where  $\overline{L_y}$  is the mean breadth of the roughness elements perpendicular to the wind direction,  $\overline{H}$  is the mean roughness element height, and  $\square_d$  is the density (number) of roughness elements per unit area ( $\square_d = n/A_T$ ).

Similar to the plan area fraction  $\square_p$ , the value of  $\square_f$  will be dependent on the location and the size of the area selected for analysis. Therefore, we have calculated  $\square_f$  for several different sized areas and as a function of land use. In addition, there is some ambiguity regarding the minimum distance between two adjacent buildings that should be used to distinguish the buildings as two separate buildings. The issue is that as two buildings are placed closer together the upstream building may start to mask the frontal face of the downstream building. For some applications, knowing the exposed frontal area may be more important than knowing the total frontal area. For example, for a cluster of buildings the drag may be better correlated to exposed frontal area as compared to total frontal area. For this study, we consider two separate buildings to be a single building only if the adjacent faces are touching. Using this rule we calculated the  $\square_f$  using the Avenue scripts for the entire 16.7-km² study area assuming the wind was approaching the city from the north, northeast, east, southeast, south, southwest, west, and northwest.

*Results*. Table 6 lists the computed  $\square_f$  values for the 16.7-km² study area for eight approach wind directions. For this large study area (i.e., an area with many buildings)  $\square_f$  is only slightly sensitive to approach flow wind direction. Because of the symmetrical characteristics of buildings it is expected that opposite wind directions (e.g., North and South) will have nearly identical frontal area indices. For our study area, the majority of streets run in the N-S and E-W directions. Hence, the along street directions are north, east, south, and west directions and have slightly smaller values.

**Table 6.** Summary of frontal area index ( $\square_f$ ) for downtown Phoenix for several wind approach directions.

	North	Northeast	East	Southeast	South	Southwest	West	Northwest
∏f	0.06	0.08	0.06	0.08	0.06	0.08	0.06	0.08

The value of  $\square_f$  is expected to be a function of land use because of the differences in building characteristics between different land uses. The relationship is also expected to be variable for samples of the same type of land use where building characteristics are highly variable, e.g., Urban High-rise, but not so variable for fairly homogeneous and consistent land uses, e.g., Single-family High-density Residential. Table 7 shows the  $\square_f$  values calculated for each land use

type. Table 8 compares the computed  $\square_f$  for several land uses in Phoenix to the computed  $\square_f$  for other cities and land uses. Note that we have not included trees in our calculation of the frontal area index, but several of the other studies cited in Table 8 have included trees.

Figure 24 shows the frontal area index for a north wind azimuth spatially distributed according to the non-uniform grid cell mesh. Calculations were not possible for the uniform 100-m X 100-m mesh because the grid cells are smaller than several buildings and buildings cross grid cell boundaries. This causes problems when trying to calculate the projected wall area in the grid cell. Some cells do not contain any walls because they are completely within the building. Rather than trying to develop a method to calculate  $\prod$  for these instances we decided to forego the calculation of  $\prod$  for the uniform grid cell mesh. Similar to the plan area fraction, we see smaller frontal area index values computed for areas including highway. Different from the plan area fraction distribution, we see the highest computed frontal area index values in the high-rise city center area, and lower values in the industrial regions. In general, the study area has a significant variation in computed frontal area index values. Several grid cells have computed values near zero, while several have computed values greater than 0.5. A direct relationship between land use and frontal area index is not demonstrated in this study area. Although we note the general trend of higher than average frontal area index values in the high-rise areas, this is not universal. For example, several grid cells contain tall buildings with small plan area fractions compared to the grid cell plan area, which results in a smaller than average frontal area index.

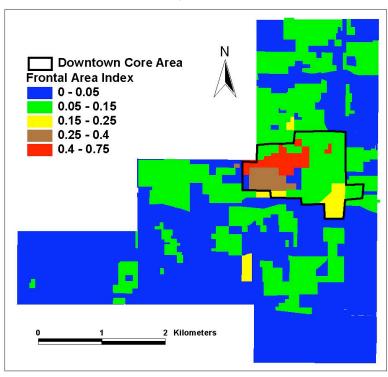
**Table 7.** Frontal area index  $(\underline{\Gamma}_f)$  as a function of land use type. Four approach wind directions are included in the table.

Land Use Class	North	Northeast	East	Southeast
Residential	0.04	0.06	0.04	0.06
Low-density Single-family (< 8 units/hectare)				
High-density Single-family (≥ 8 units/hectare)	0.04	0.05	0.04	0.05
Multifamily	0.06	0.08	0.06	0.08
Mixed				
Commercial & Services	0.09	0.12	0.09	0.12
Non-high-rise				
High-rise				
Industrial	0.04	0.06	0.04	0.06
Transportation/Communications/Utilities	0.00	0.00	0.00	0.00
Mixed Industrial & Commercial				
Mixed Urban or Built-up				
Other Urban or Built-up	0.01	0.02	0.01	0.02
Predominantly Vegetated	0.01	0.02	0.01	0.02
Predominantly Built-up				
Urban High-rise				
Downtown Core Area	0.20	0.26	0.19	0.26

 Table 8. Comparison of frontal area index (☐) for several cities and land uses

Location	Land Use Class	∐f	Source
Arcadia, CA	Suburban residential	0.33	Grimmond and Oke (1999)
Chicago, IL	Suburban residential	0.28	Grimmond and Oke (1999)
Los Angeles, CA	Multifamily residential	0.25	Burian et al. (2002b)*
Salt Lake City, UT	Multifamily residential	0.25	Burian et al. (2002c)*
Sacramento, CA	Suburban residential	0.23	Grimmond and Oke (1999)
Chicago, IL	Suburban residential	0.21	Grimmond and Oke (1999)
Tucson, AZ	Suburban residential	0.19	Grimmond and Oke (1999)
Vancouver, BC, Canada	Suburban residential	0.19	Grimmond and Oke (1999)
Miami, FL	Suburban residential	0.16	Grimmond and Oke (1999)
San Gabriel, CA	Suburban residential	0.14	Grimmond and Oke (1999)
Los Angeles, CA	High-density single-family residential	0.12	Burian et al. (2002b)*
Phoenix, AZ	High-density single-family residential	0.05	This Report*
Salt Lake City, UT	Industrial	0.15	Burian et al. (2002c)*
Vancouver, BC, Canada	Light industrial	0.13	Grimmond and Oke (1999)
Los Angeles, CA	Industrial	0.10	Burian et al. (2002b)*
Phoenix, AZ	Industrial	0.05	This Report*
Los Angeles, CA	Urban high-rise	0.45	Burian et al. (2002b)*
Los Angeles, CA	Downtown core area	0.38	Burian et al. (2002b)*
Salt Lake City, UT	Urban high-rise	0.32	Burian et al. (2002c)*
Vancouver, BC, Canada	Central city	0.30	Grimmond and Oke (1999)
Phoenix, AZ	Downtown Core Area	0.23	This Report*
Mexico City, Mexico	Central city	0.19	Grimmond and Oke (1999)
Los Angeles, CA	Non-high-rise commercial & services	0.13	Burian et al. (2002b)*

<sup>\*</sup>The values shown from this study are the average values for eight wind directions (north, northeast, east, southeast, south, southwest, west, northwest).



**Figure 24.** Spatial distribution of building frontal area index  $(\Box_f)$  for a north wind azimuth.

#### 4.6 Frontal Area Density (a<sub>f</sub>(z))

*Background*. The frontal area is often used in computing the drag force on solid objects immersed in fluids. The frontal area density, a measure of the frontal area per unit horizontal area per unit height increment, has been used by researchers in the plant canopy and urban canopy communities to help quantify the drag force as a function of height. The drag force approach allows one to compute the area-averaged wind profile within the canopy.

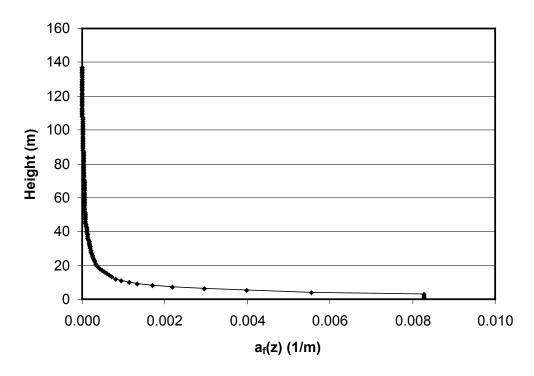
Calculation Methods. The frontal area density  $(a_1(z))$  is defined as:

$$a_f(z, \square) = \frac{A(\square)_{proj(\square z)}}{A_T \square z} \tag{14}$$

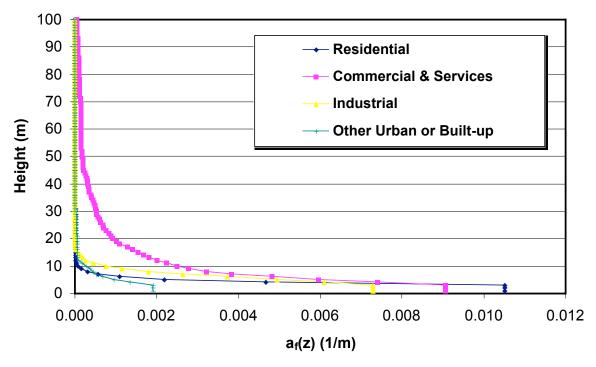
where  $A(\square_{proj(\square^2)})$  is the area of building surfaces projected into the plane normal to the approaching wind direction for a specified height increment  $(\square z)$ ,  $\square$  is the wind direction angle, and  $A_T$  is the total plan area of the study site. For a specified wind direction, the integral of  $a_f(z)$  over the canopy height equates to  $\square_f$ :

Results. We performed the frontal area density calculations at one-meter increments. Figure 25 shows  $a_f(z)$  for the Phoenix study area for a wind approaching from the north. Figure 26 shows the  $a_f(z)$  functions for the land use types in the 7-category scheme that have a sufficient number of buildings and land area to produce meaningful results. Figure 27 shows the  $a_f(z)$  functions for the 12-category land use scheme and the Downtown Core Area.

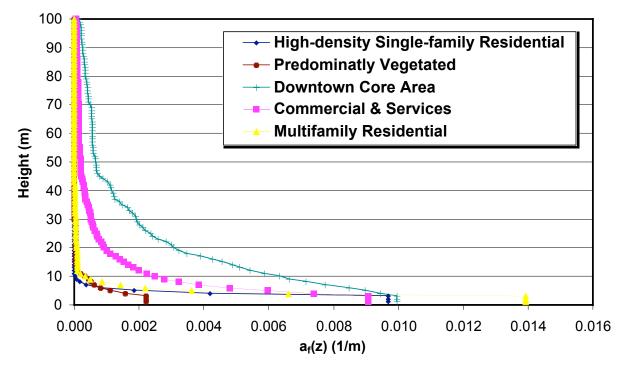
Interestingly, the frontal area density near the ground is largest for Residential areas. This occurs due to the preponderance of shorter buildings in Residential areas (many short buildings occupying the same volume as a few taller buildings have more frontal area). Commercial & Services has a higher frontal area density near the ground surface than Industrial land use. Presumably Industrial has a relatively low frontal area density near the surface due to wide, squat buildings, like warehouses with large open parking lots. The frontal area density decays most rapidly with height for Residential and Industrial areas due to low building heights. The Downtown Core Area land use decays most slowly with height due to the large number of tall buildings in this land use type.



**Figure 25.** Frontal area density function  $(a_f(z))$  for the Phoenix study area for a wind approaching from the north.



**Figure 26.** Frontal area density function  $(a_f(z))$  for land use types in the 7-category scheme for a wind approaching from the north.



**Figure 27.** Frontal area density function  $(a_f(z))$  for several land use types in the 12-category scheme and the Downtown Core Area land uses for a wind approaching from the north.

# 4.7 Complete Aspect Ratio (□c)

*Background*. The "complete" surface area, including building walls, roofs, and ground surfaces, is important when evaluating the urban canopy energy budget in a city. All of these surfaces act as sources and sinks of heat and need to be accounted for when evaluating the energy balance of an urbanized area. The non-dimensional form of the complete surface area, the complete aspect ratio, is useful in interpreting surface temperatures derived from remote sensing instruments. Used with the plan area  $\square_p$ , some notion of the three-dimensionality of the urban fabric can be obtained and better estimates of the "real" skin temperature might be computed.

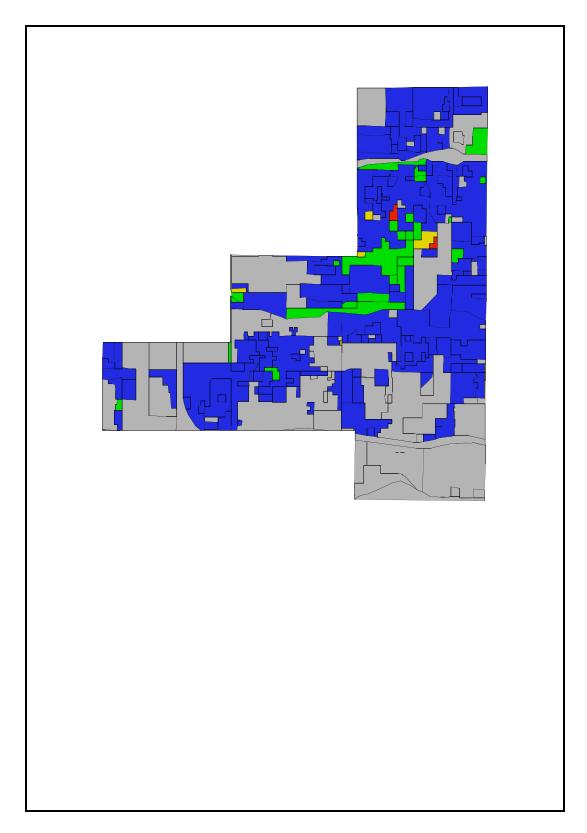
Calculation Methods. The complete aspect ratio ( $\square_C$ ) is defined as the summed surface area of roughness elements and exposed ground divided by the total plan area (Voogt and Oke 1997):

$$\Box_C = \frac{A_C}{A_T} = \frac{A_W + A_R + A_G}{A_T} \tag{15}$$

where  $A_C$  is the combined surface area of the buildings and exposed ground,  $A_W$  is the wall surface area,  $A_R$  is the roof area,  $A_G$  is the area of exposed ground, and  $A_T$  is the plan area of the study site.  $A_C$  is calculated by summing the surface area of the buildings and the difference between the total plan area of the site and the plan area of buildings at ground level (i.e., the exposed ground surface). For dense urban areas with flat roofed buildings and without much vegetation,  $A_C$  can be approximated as the sum of the plan area of the site and the area of building walls (not including rooftops).

Using an Avenue script in the ArcView GIS we automatically calculated  $\square_c$  for the entire city for a non-uniform grid cell mesh (shown in Figure 15) and as a function of land use. Calculations were not possible for the uniform 100-m X 100-m mesh for the same reasons described for frontal area index. The rooftop surface area was calculated assuming the rooftops were flat, which a digital orthophoto indicated to be true for most of the land use types, except for some of the High-density Single-family Residential areas. Another source of error in our complete aspect ratio calculation is the neglect of the surface area of trees and bushes. Grimmond and Oke (1999) found the surface area of trees and bushes to be an important component of the complete surface area, especially in residential areas.

*Results*. For the 16.7-km<sup>2</sup> study area, the  $\square_C$  was calculated to be 1.51. The  $\square_C$  for each grid cell was calculated for the non-uniform grid cell mesh (Figure 28). For the non-uniform mesh, the mean  $\square_C$  was 1.15, with a standard deviation of 0.27, and a range of 1.0 to 4.52. The high-rise area is located within the conglomeration of red grid cells in Figure 28. The computed  $\square_C$  values for each land use type in our classification schemes are shown in Table 9. The  $\square_C$  values for the downtown area are in the range of 1.25 to 4.52, which are consistent with the central city values from other studies shown in Table 10.



**Figure 28.** Display of complete aspect ratio ( $\square_C$ ) calculated for the Phoenix downtown area per grid cell.

**Table 9.** Complete aspect ratio ( $\square_c$ ) for each land use type

Land Use Class	$\Box c$
Residential	1.16
Low-density Single-family (< 8 units/hectare)	
High-density Single-family (≥ 8 units/hectare)	1.14
Multifamily	1.23
Mixed	
Commercial & Services	1.35
Non-high-rise	
High-rise	
Industrial	1.17
Transportation/Communications/Utilities	0
Mixed Industrial & Commercial	
Mixed Urban or Built-up	
Other Urban or Built-up	1.06
Predominantly Vegetated	1.06
Predominantly Built-up	
Urban High-rise	
Downtown Core Area	1.75

Table 10 compares selected values from Table 9 with  $\square_C$  values computed for other cities. The  $\square_C$  computed for Phoenix Residential land use is lower than those found for other cities. The  $\square_C$  computed for the Industrial land use type in the Phoenix study area is greater than the value computed for a light industrial area in Vancouver. The Downtown Core Area land use types in Phoenix has a lower  $\square_C$  value than values computed for most other cities.

**Table 10.** Complete aspect ratio  $( \square_c )$  for downtown Phoenix and other cities

Location	Land Use Class	□c	Source
Salt Lake City, UT	Multifamily residential	1.89	Burian et al. (2002c)
Arcadia, CA	Suburban residential	1.78	Grimmond and Oke (1999)
Los Angeles, CA	Multifamily residential	1.77	Burian et al. (2002b)
Chicago, IL	Suburban residential	1.74	Grimmond and Oke (1999)
Vancouver, BC, Canada	Suburban residential	1.65	Voogt and Oke (1997)
Salt Lake City, UT	High-density single-family residential	1.65	Burian et al. (2002c)
Sacramento, CA	Suburban residential	1.63	Grimmond and Oke (1999)
Chicago, IL	Suburban residential	1.51	Grimmond and Oke (1999)
Tucson, AZ	Suburban residential	1.45	Grimmond and Oke (1999)
Miami, FL	Suburban residential	1.37	Grimmond and Oke (1999)
Los Angeles, CA	High-density single-family residential	1.36	Burian et al. (2002b)
San Gabriel, CA	Suburban residential	1.31	Grimmond and Oke (1999)
Phoenix, AZ	High-density single-family residential	1.14	This Report
Salt Lake City, UT	Industrial	1.48	Burian et al. (2002c)
Salt Lake City, UT Vancouver, BC, Canada	Industrial Light industrial	1.48 1.39	Burian et al. (2002c) Voogt and Oke (1997)
			` '
Vancouver, BC, Canada	Light industrial	1.39	Voogt and Oke (1997)
Vancouver, BC, Canada Los Angeles, CA	Light industrial Industrial	1.39 1.30	Voogt and Oke (1997) Burian et al. (2002b)
Vancouver, BC, Canada Los Angeles, CA Phoenix, AZ	Light industrial Industrial Industrial	1.39 1.30 <b>1.17</b>	Voogt and Oke (1997) Burian et al. (2002b) This Report
Vancouver, BC, Canada Los Angeles, CA Phoenix, AZ Los Angeles, CA	Light industrial Industrial Industrial High-rise commercial & services	1.39 1.30 <b>1.17</b> 2.60	Voogt and Oke (1997) Burian et al. (2002b) This Report Burian et al. (2002b)
Vancouver, BC, Canada Los Angeles, CA Phoenix, AZ Los Angeles, CA Los Angeles, CA	Light industrial Industrial Industrial High-rise commercial & services Urban high-rise	1.39 1.30 <b>1.17</b> 2.60 2.44	Voogt and Oke (1997) Burian et al. (2002b) This Report Burian et al. (2002b) Burian et al. (2002b)
Vancouver, BC, Canada Los Angeles, CA Phoenix, AZ Los Angeles, CA Los Angeles, CA Los Angeles, CA	Light industrial Industrial Industrial High-rise commercial & services Urban high-rise Downtown core area	1.39 1.30 1.17 2.60 2.44 2.22	Voogt and Oke (1997) Burian et al. (2002b) This Report Burian et al. (2002b) Burian et al. (2002b) Burian et al. (2002b)
Vancouver, BC, Canada Los Angeles, CA Phoenix, AZ Los Angeles, CA Los Angeles, CA Los Angeles, CA Vancouver, BC, Canada	Light industrial Industrial Industrial High-rise commercial & services Urban high-rise Downtown core area Central city	1.39 1.30 1.17 2.60 2.44 2.22 2.20	Voogt and Oke (1997) Burian et al. (2002b) This Report Burian et al. (2002b) Burian et al. (2002b) Burian et al. (2002b) Voogt and Oke (1997)
Vancouver, BC, Canada Los Angeles, CA Phoenix, AZ Los Angeles, CA Los Angeles, CA Los Angeles, CA Vancouver, BC, Canada Salt Lake City, UT	Light industrial Industrial Industrial Industrial High-rise commercial & services Urban high-rise Downtown core area Central city Urban high-rise	1.39 1.30 1.17 2.60 2.44 2.22 2.20 2.05	Voogt and Oke (1997) Burian et al. (2002b) This Report Burian et al. (2002b) Burian et al. (2002b) Burian et al. (2002b) Voogt and Oke (1997) Burian et al. (2002c)

# 4.8 Building Surface Area to Plan Area Ratio ([]<sub>B</sub>)

Background. Another measure of urban terrain character is the ratio of built surface area to the plan surface area. Like the complete aspect ratio (Section 4.7), the building surface area is important when evaluating the urban canopy energy budget in a city. Building walls and roof surfaces act as sources and sinks of heat and need to be accounted for when evaluating the energy balance of an urbanized area. Perhaps some combination of frontal area, plan area, complete surface area, and building surface area parameters will allow for better parameterizations of the urban canopy energy budget.

Calculation Methods. The building surface area to plan area ratio ( $\square$ ) is defined as the sum of building surface area divided by the total plan area:

$$\square_{B} = \frac{A_R + A_W}{A_T} \tag{16}$$

where  $A_R$  is the plan area of rooftops,  $A_W$  is the total area of non-horizontal roughness element surfaces (e.g., walls), and  $A_T$  is the total plan area of the study location. For the calculations below, we have made a flat-roof assumption.

*Results*. The  $\square_B$  for the 16.7-km<sup>2</sup> study area in Phoenix was calculated to be 0.82. Table 11 shows the computed  $\square_B$  values for each land use type included in the building analysis. Commercial & Services and Downtown Core Area have the largest values due to the presence of tall buildings and fairly high plan area fraction. We did not find values for other cities for this parameter.

**Table 11.** Building surface area to plan area ratio  $(\Gamma_B)$  for each land use type

Land Use Class	□в
Residential	0.29
Low-density Single-family (< 8 units/hectare)	
High-density Single-family (≥ 8 units/hectare)	0.26
Multifamily	0.41
Mixed	
Commercial & Services	0.55
Non-high-rise	
High-rise	
Industrial	0.36
Transportation/Communications/Utilities	0
Mixed Industrial & Commercial	
Mixed Urban or Built-up	
Other Urban or Built-up	0.08
Predominantly Vegetated	0.10
Predominantly Built-up	
Urban High-rise	
Downtown Core Area	1.07

# 4.9 Height-to-Width Ratio (□s)

Background. The ratio of the height of buildings to the horizontal distance (or street width) between the buildings is called the height-to-width ratio ( $\square$ s). The height-to-width ratio has been found, for idealized arrangements of same-height buildings, to influence the flow regime. Hussain and Lee (1980) performed wind-tunnel experiments and found the three flow regimes develop in idealized urban street canyons: (1) isolated flow, (2) wake interference flow, and (3) skimming flow. The isolated flow regime occurs when elements are spaced relatively far apart ( $\square$ s < 0.4), the wake interference flow occurs when elements are spaced at a medium density level (0.4 <  $\square$ s < 0.7), and the skimming flow regime occurs for high-density building arrangements ( $\square$ s > 0.7) (Oke 1988).

Calculation Methods. The height-to-width ratio ( $\square$ s) (also called the street aspect ratio) is calculated for two buildings by dividing the average height by the distance between the two buildings:

$$\Box_{S} = \frac{(H_{1} + H_{2})/2}{S_{12}} \tag{17}$$

where  $H_1$  is the height of the upwind building,  $H_2$  is the height of the downwind building, and  $S_{12}$  is the horizontal distance between the two buildings (i.e., the canyon width). Figure 29 illustrates the measures used to compute  $\square_S$ . The calculation of  $\square_S$  is performed for each pair of adjacent elements in a building array, which can be very tedious for the complex building shapes and patterns in a city. For idealized arrangements of buildings, the calculation of an average  $\square_S$  can be approximated by taking the average building height divided by the average width between buildings (Grimmond and Oke 1999):

$$\overline{\square}_{S} \, \square \, \frac{\overline{Z_{H}}}{\overline{W}} \tag{18}$$

where  $\overline{z_{\scriptscriptstyle H}}$  is the average building height and  $\overline{W}$  is the average distance between buildings.

Due to the large number of buildings in the Phoenix dataset, an automated approach is warranted. Because of the complexity of the Phoenix downtown area, we did not use the simplified methodology described by Eqn. (18). Instead, we computed  $\square_S$  along linear traverses across the city at different angles using Eqn. (17). Our calculation strategy involved converting the urban building database into a raster digital elevation model (DEM – a matrix of numbers representing building height). Then traversing along each row or column of grid cells the height-to-width ratio was calculated between each pair of buildings. A Fortran code was written to execute this procedure. Since this approach yields  $\square_S$  values in non-preferred directions (e.g., running along a street, not across a street), we then superimposed the matrices of traverses done at different angles, and chose the height-to-width ratio at each grid cell by selecting the largest value.

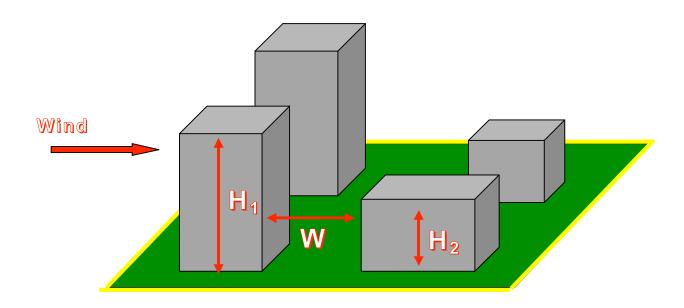
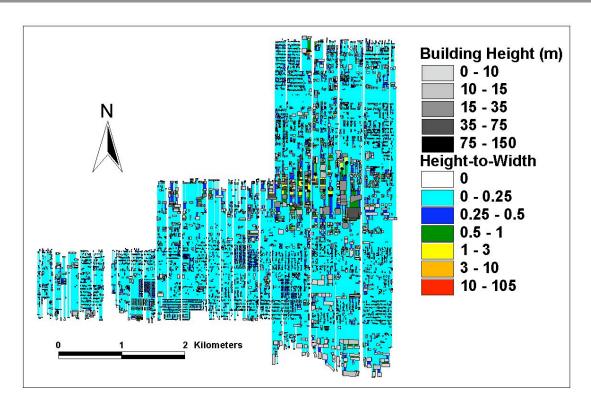


Figure 29. Illustration of height-to-width ratio parameter.

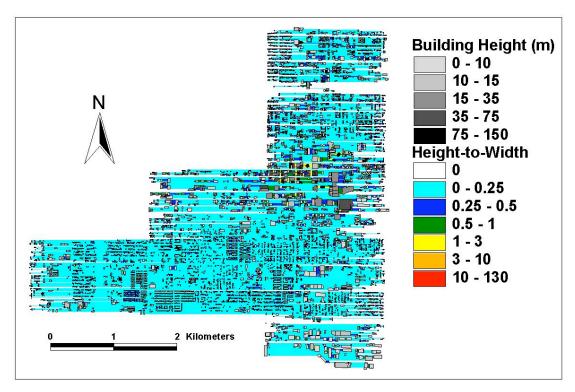
Figures 30 and 31 show the spatial distribution of the computed  $\square_S$  values for the two analysis directions that corresponded with the predominant street directions. Due to the unidirectional nature of the traverses, one can plainly see that the height-to-width ratio is too small between some buildings. For example, in Fig. 30 the  $\square_S$  values are underestimated along the south-to-north-running streets. Figure 32 shows the composite  $\square_S$  values, which were computed at each grid cell by selecting the largest value from the superimposed matrices from the two traversal directions, i.e., superimposing the values from Figs. 30 and 31. The higher  $\square_S$  values are clearly visible in the downtown area of Phoenix (the buildings are shaded by height).

Figures 33, 34, and 35 show the composite  $\square_S$  values for areas predominantly composed of Residential, Industrial, and Downtown Core Area land uses, respectively. The figures clearly illustrate the concentration of the highest  $\square_S$  values in the high-rise area. The  $\square_S$  values are fairly similar for the Residential and Industrial land uses.

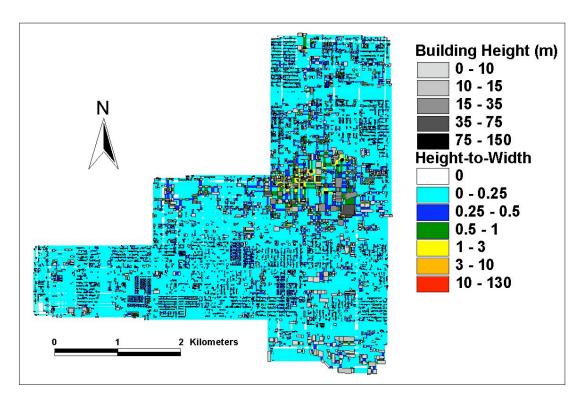
We also computed the average  $\square_S$  values for the study area and for each land use type in our classification schemes. The average  $\square_S$  was computed by using the area-weighted average of the spatial distribution of the composite height-to-width ratio shown in Figure 32. One could also weight the average  $\square_S$  by number of buildings, streets, or some other quantity. In the approach used here, buildings with larger footprints will exert a greater influence over the area-weighted average. In addition, open areas (e.g., parking lots and parks) and street intersections will be counted in the average.



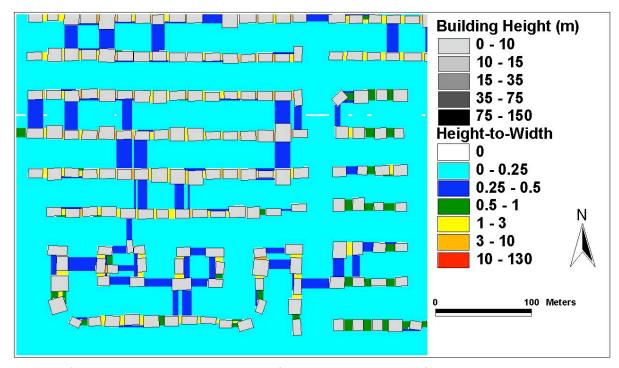
**Figure 30.** Computed height-to-width ratio ( $\square$ <sub>S</sub>) for the Phoenix study area (analysis traversal was from the north to south).



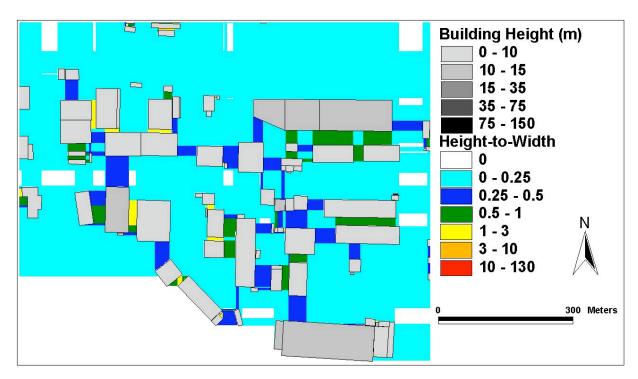
**Figure 31.** Computed height-to-width ratio ( $\square$ s) for the Phoenix study area (analysis traversal was from the west to the east).



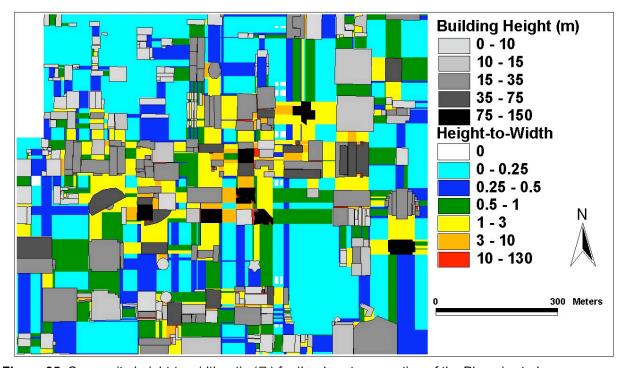
**Figure 32.** Composite height-to-width ratio ( $\square_S$ ) for the Phoenix study area based on the integration of computed values for the two analysis traversals.



**Figure 33.** Composite height-to-width ratio ( $\square_s$ ) for a residential section of the Phoenix study area.



**Figure 34.** Composite height-to-width ratio ( $\square_S$ ) for an industrial section of the Phoenix study area.



**Figure 35.** Composite height-to-width ratio ( $\square$ s) for the downtown section of the Phoenix study area.

*Results*. The area-weighted average  $\square_S$  for the study area was calculated to be 0.18. The range of  $\square_S$  for the study area was 0 to 127.3. Zero values occur where buildings are located and in regions where two buildings do not lie on an 'along-the-street' or 'across-the-street' transect. Table 12 lists the area-weighted average  $\square_S$  values for each land use type.

**Table 12.** Area-weighted average composite height-to-width ratio (□s)

Land Use Class	∐s
Residential	0.16
Low-density Single-family (< 8 units/hectare)	
High-density Single-family (≥ 8 units/hectare)	0.14
Multifamily	0.22
Mixed	
Commercial & Services	0.26
Non-high-rise	
High-rise	
Industrial	0.13
Transportation/Communications/Utilities	0.04
Mixed Industrial & Commercial	
Mixed Urban or Built-up	
Other Urban or Built-up	0.07
Predominantly Vegetated	0.07
Predominantly Built-up	0.02
Urban High-rise	
Downtown Core Area	0.60

Table 13 compares selected values from our study with values computed for other cities. The values we calculated for Phoenix are on the lower end of the range of values from other cities. The relatively small values can be partially attributed to the more modern development style of Phoenix with lower height dwellings with more open space. Also, the averaging scheme could cause significant differences; sensitivity studies need to be performed.

**Table 13.** Comparison of height-to-width ( $\square$ s) for Phoenix and other cities

Location	Land Use Class	∐s	Source
Sacramento, CA	Suburban residential	1.21	Grimmond and Oke (1999)
Arcadia, CA	Suburban residential	1.19	Grimmond and Oke (1999)
Miami, FL	Suburban residential	1.03	Grimmond and Oke (1999)
Chicago, IL	Suburban residential	0.97	Grimmond and Oke (1999)
Vancouver, BC, Canada	Suburban residential	0.90	Grimmond and Oke (1999)
Tucson, AZ	Suburban residential	0.54	Grimmond and Oke (1999)
Salt Lake City, UT	Multifamily residential	0.47	Burian et al. (2002c)
Los Angeles, CA	Multifamily residential	0.45	Burian et al. (2002b)
San Gabriel, CA	Suburban residential	0.43	Grimmond and Oke (1999)
Los Angeles, CA	High-density single-family residential	0.23	Burian et al. (2002b)
Dhamir A7	Multifossilus socialostial	0.00	This Demant
Phoenix, AZ	Multifamily residential	0.22	This Report
Vancouver, BC, Canada	Light industrial	0.22	Grimmond and Oke (1999)
			·
Vancouver, BC, Canada	Light industrial	0.57	Grimmond and Oke (1999)
Vancouver, BC, Canada Salt Lake City, UT	Light industrial Industrial	0.57 0.23	Grimmond and Oke (1999) Burian et al. (2002c)
Vancouver, BC, Canada Salt Lake City, UT Los Angeles, CA	Light industrial Industrial Industrial	0.57 0.23 0.20	Grimmond and Oke (1999) Burian et al. (2002c) Burian et al. (2002b)
Vancouver, BC, Canada Salt Lake City, UT Los Angeles, CA Phoenix, AZ	Light industrial Industrial Industrial Industrial	0.57 0.23 0.20 <b>0.13</b>	Grimmond and Oke (1999) Burian et al. (2002c) Burian et al. (2002b) This Report
Vancouver, BC, Canada Salt Lake City, UT Los Angeles, CA Phoenix, AZ Vancouver, BC, Canada	Light industrial Industrial Industrial Industrial Central city	0.57 0.23 0.20 <b>0.13</b> 1.40	Grimmond and Oke (1999) Burian et al. (2002c) Burian et al. (2002b) This Report Grimmond and Oke (1999)
Vancouver, BC, Canada Salt Lake City, UT Los Angeles, CA Phoenix, AZ Vancouver, BC, Canada Mexico City, Mexico	Light industrial Industrial Industrial Industrial Central city Central city Commercial & services	0.57 0.23 0.20 <b>0.13</b> 1.40 1.19	Grimmond and Oke (1999) Burian et al. (2002c) Burian et al. (2002b) This Report Grimmond and Oke (1999) Grimmond and Oke (1999)
Vancouver, BC, Canada Salt Lake City, UT Los Angeles, CA Phoenix, AZ Vancouver, BC, Canada Mexico City, Mexico Los Angeles, CA	Light industrial Industrial Industrial Industrial Central city Central city Commercial & services high-rise	0.57 0.23 0.20 <b>0.13</b> 1.40 1.19 0.91	Grimmond and Oke (1999) Burian et al. (2002c) Burian et al. (2002b) This Report Grimmond and Oke (1999) Grimmond and Oke (1999) Burian et al. (2002b)

## 4.10 Aerodynamic Roughness Parameters

Background. The representation of surface roughness is a critical first step in many meteorological, wind engineering, and pollutant dispersion modeling activities. It provides an estimate of the drag and turbulent mixing associated with the underlying surface. The displacement height  $(z_d)$  and roughness length  $(z_o)$  are key parameters in the logarithmic velocity profile based on similarity theory and is commonly used in many models to specify the boundary conditions above built-up areas. The displacement height can be conceptualized as the height of a surface formed by distributing the aggregate volume of roughness elements and their wake recirculation cavities uniformly over the underlying surface (Macdonald et al. 1998). The roughness length is directly related to the overall drag of the surface. Mathematically, it represents the distance above the displacement height plane at which the velocity goes to zero.

Both  $z_d$  and  $z_o$  are difficult to estimate with certainty by experiment or theory. Grimmond and Oke (1999) reviewed methods to calculate the  $z_d$  and  $z_o$  of urban areas based on building and vegetation morphology. They compared the predictions of the morphological methods to those obtained from wind measurements in urban areas. Using the equations rated amongst the most appropriate by Grimmond and Oke (1999), we calculated values of  $z_d$  and  $z_o$  for the entire Phoenix study area, spatially over a defined grid and as a function of land use in the study area. Note that the similarity theory is not valid in horizontally inhomogeneous areas and that for many urban areas the roughness parameter concept will not hold or can only be applied well above the roughness elements.

Calculation Methods. A common method used to calculate the displacement height  $(z_d)$  and roughness length  $(z_o)$  are simple rules-of-thumb (Grimmond and Oke 1999):

$$z_d = f_d \overline{z_H} \tag{19}$$

and

$$z_o = f_o \overline{z_H} \tag{20}$$

where  $\overline{z_H}$  is the average building height and  $f_d$  and  $f_o$  are empirical coefficients. Approximations for urban values are 0.5 for  $f_d$  and 0.1 for  $f_o$ . Beyond the limitations of applying these equations to horizontally inhomogeneous urban areas, these equations also only hold for medium building density situations, as it is known that  $z_o$  and  $z_d$  vary with building spacing.

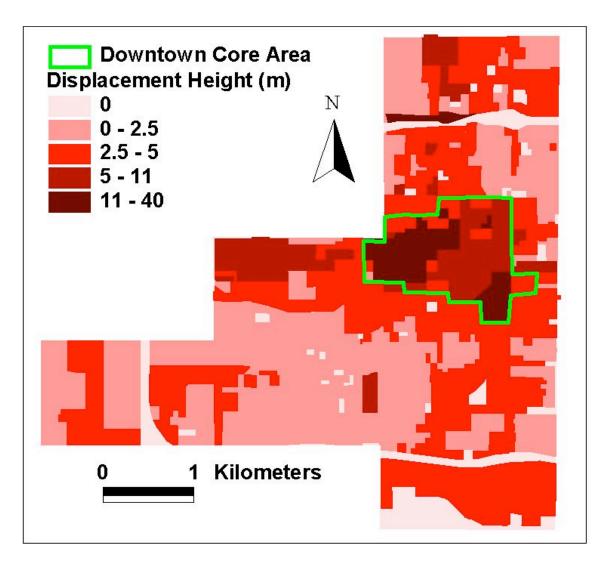
Results. Although Eqns. (19) and (20) may not hold for all areas in our study domain, we have still computed the aerodynamic roughness parameters for the Phoenix study area for comparison purposes. Using these approximations we found that  $z_d \, \Box \, 2.80$  m and  $z_o \, \Box \, 0.56$  m when using the mean building height, and  $z_d \, \Box \, 4.60$  m and  $z_o \, \Box \, 0.92$  m when using the plan-area-weighted average building height. Table 14 lists the computed  $z_d$  and  $z_o$  values for each land use type using the mean building height and Eqns. (19) and (20). Table 15 lists the computed  $z_d$  and  $z_o$  values for each land use type using the plan-area-weighted average building height and Eqns. (19) and (20), while Figures 36 and 37 show the spatial distribution of the  $z_d$  and  $z_o$ .

**Table 14.** Displacement height  $(z_d)$  and roughness length  $(z_o)$ : simple rules-of-thumb eqns. and average building height

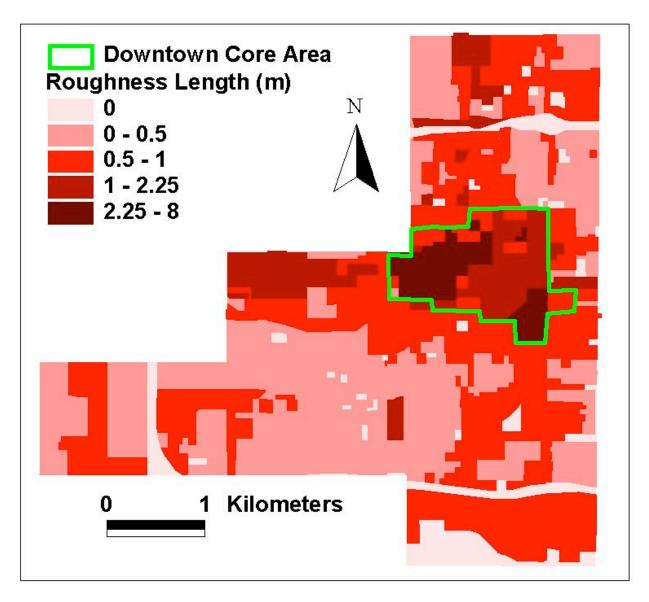
Land Use Class	$z_d$ (m)	$z_o$ (m)
Residential	1.89	0.38
Low-density Single-family (< 8 units/hectare)		
High-density Single-family (≥ 8 units/hectare)	1.84	0.37
Multifamily	2.09	0.42
Mixed		
Commercial & Services	4.29	0.86
Non-high-rise		
High-rise		
Industrial	2.57	0.51
Transportation/Communications/Utilities	0	0
Mixed Industrial & Commercial		
Mixed Urban or Built-up		
Other Urban or Built-up	2.71	0.54
Predominantly Vegetated	2.71	0.54
Predominantly Built-up		
Urban High-rise		
Downtown Core Area	8.65	1.73

**Table 15.** Displacement height  $(z_d)$  and roughness length  $(z_o)$ : simple rules-of-thumb eqns. and plan-area-weighted average building height

Land Use Class	z <sub>d</sub> (m)	$z_o$ (m)
Residential	2.07	0.41
Low-density Single-family (< 8 units/hectare)		
High-density Single-family (≥ 8 units/hectare)	1.96	0.39
Multifamily	2.35	0.47
Mixed		
Commercial & Services	6.53	1.31
Non-high-rise		
High-rise		
Industrial	3.55	0.71
Transportation/Communications/Utilities	0	0
Mixed Industrial & Commercial		
Mixed Urban or Built-up		
Other Urban or Built-up	4.18	0.84
Predominantly Vegetated	4.18	0.84
Predominantly Built-up		
Urban High-rise		
Downtown Core Area	10.59	2.12



**Figure 36.** Spatial distribution of displacement height ( $z_d$ ) in downtown Phoenix computed using the simple rule-of-thumb (Eqn. (19)) and the plan-area-weighted average building height.



**Figure 37.** Spatial distribution of the roughness length ( $z_o$ ) in downtown Phoenix computed using the simple rule-of-thumb (Eqn. 20) and the plan area-weighted average building height.

Calculation Methods. We also computed the  $z_d$  and  $z_o$  using two more complex equations described by Grimmond and Oke (1999). Although they compared results produced by different equations and concluded that it is difficult to measure their predictive accuracy, they did suggest an ordering of the morphometric equations. One set of equations ranked highly were those developed by Raupach (1994):

$$\frac{z_d}{\overline{z}_H} = 1 \square \left[ \frac{1 \square \exp \left[ \square \left( c_{d1} 2 \square_f \right)^{0.5} \right]}{\left( c_{d1} 2 \square_f \right)^{0.5}} \right]$$
(21)

and

$$\frac{z_o}{z_H} = \left[ \frac{z_d}{z_H} \right] \exp \left[ \frac{z_d}{z_H} + \frac{U}{u_0} \right]$$
 (22)

where

$$\frac{u_{\square}}{U} = \min \left[ \left( c_S + c_R \square_f \right)^{0.5}, \square \right] \frac{u_{\square}}{U} = \prod_{\text{max}} \square$$
(23)

and  $\Box_k$  is the roughness sublayer influence function, U and  $u_*$  are the large-scale wind speed and the friction velocity, respectively,  $c_S$  and  $c_R$  are drag coefficients for the substrate surface at height  $z_H$  in the absence of roughness elements and of an isolated roughness element mounted on the surface, respectively, and  $c_{d1}$  is a free parameter. Raupach (1994) suggested  $\Box_k = 0.193$ ,  $(u_*/U)_{max} = 0.3$ ,  $c_S = 0.003$ ,  $c_R = 0.3$ , and  $c_{d1} = 7.5$ .

Results. Using these values, a von Kármán constant (k) of 0.4, and the values computed for the average building height and the average frontal area index, we calculated  $z_d \, \Box \, 2.10$  m and  $z_o \, \Box \, 0.32$  m. When using the plan-area-weighted average building height we found  $z_d \, \Box \, 3.44$  m and  $z_o \, \Box \, 0.53$  m. These values are very similar to those derived using the simple scheme described above (Eqns. (19) and (20)). Tables 16 and 17 list the computed  $z_d$  and  $z_o$  for each land use type using the average building height and the plan-area-weighted average building height, respectively.

**Table 16.** Displacement height  $(z_d)$  and roughness length  $(z_o)$ : Raupach (1994) equations with the average building height

Land Use Class	$z_d$ (m)	$z_o$ (m)
Residential	1.25	0.16
Low-density Single-family (< 8 units/hectare)		
High-density Single-family (≥ 8 units/hectare)	1.17	0.14
Multifamily	1.57	0.24
Mixed		
Commercial & Services	3.75	0.71
Non-high-rise		
High-rise		
Industrial	1.70	0.21
Transportation/Communications/Utilities	0	0
Mixed Industrial & Commercial		
Mixed Urban or Built-up		
Other Urban or Built-up	1.10	0.05
Predominantly Vegetated	1.10	0.05
Predominantly Built-up		
Urban High-rise		
Downtown Core Area	9.44	2.15

**Table 17.** Displacement height  $(z_d)$  and roughness length  $(z_o)$ : Raupach (1994) equations with the plan-area-weighted building height

Land Use Class	$z_d$ (m)	$z_o$ (m)
Residential	1.37	0.17
Low-density Single-family (< 8 units/hectare)		
High-density Single-family (≥ 8 units/hectare)	1.25	0.14
Multifamily	1.76	0.27
Mixed		
Commercial & Services	5.70	1.08
Non-high-rise		
High-rise		
Industrial	2.35	0.29
Transportation/Communications/Utilities	0	0
Mixed Industrial & Commercial		
Mixed Urban or Built-up		
Other Urban or Built-up	1.70	0.08
Predominantly Vegetated	1.70	0.08
Predominantly Built-up		
Urban High-rise		
Downtown Core Area	11.55	2.63

Calculation Methods. The second set of equations was derived by Macdonald et al. (1998). These equations incorporate the drag coefficient and displacement height into the expression for roughness length  $(z_o)$ :

$$\frac{z_d}{z_H} = 1 + \Box^{\square \mathcal{D}_p} \left( \mathcal{D}_p \ \square \ 1 \right) \tag{24}$$

and

$$\frac{z_o}{z_H} = \begin{bmatrix} 1 & \frac{z_d}{z_H} \end{bmatrix} \exp \begin{bmatrix} \frac{1}{2} & \frac{1}{2} & \frac{z_d}{z_H} \end{bmatrix} \frac{z_d}{z_H} = \begin{bmatrix} \frac{1}{2} & \frac{1}{2} & \frac{1}{2} & \frac{1}{2} \\ \frac{1}{2} & \frac{1}{2} & \frac{1}{2} & \frac{1}{2} \end{bmatrix}$$
(25)

where  $\square$  is an empirical coefficient,  $C_D$  is a drag coefficient, k is the von Kármán constant, and  $\square$  is a correction factor for the drag coefficient (the net correction for several variables, including velocity profile shape, incident turbulence intensity, turbulence length scale, and incident wind angle, and for rounded corners). Macdonald et al. (1998) recommended for staggered arrays of cubes that  $\square$  \underline{\mathbb{I}} 4.43 and  $\square$  \underline{\mathbb{I}} 1.0. These values were used by Grimmond and Oke (1999) and are also used here. We also set  $C_D = 1.2$  (the same value used Grimmond and Oke (1999) in their analysis) and the von Kármán constant k = 0.4.

Results. We found  $z_d \, \square \, 1.89$  m and  $z_o \, \square \, 0.34$  m for the Phoenix study area. Using the plan-area-weighted average building height we found  $z_d \, \square \, 3.11$  m and  $z_o \, \square \, 0.55$  m. This method gives approximately the same value for  $z_o$  compared to the values computed using the Raupach (1994) equations and slightly smaller  $z_d$  values. Tables 18 and 19 list the computed  $z_d$  and  $z_o$  for each land use for the average building height and the plan-area-weighted average building height, respectively.

Table 20 compares the computed aerodynamic roughness parameters to those calculated for other cities. The roughness parameters shown in Table 20 for Phoenix were calculated using the Raupach (1994) equations with the plan-area-weighted average building height. The values for Phoenix are comparable to values from other locations. The Multifamily Residential land use in Phoenix has a much lower displacement height and roughness length than the other cities. The displacement and roughness lengths for Industrial land use in Phoenix are near the bottom of the range, as are the Downtown Core Area values. The computed roughness length of 0.14 m for the tract of High-density Single-family Residential using the Raupach (1994) equations is outside the lower limit of the range of 0.4-0.7 m presented by Wieringa (1993) for homogeneous suburban low buildings. This suggests the Phoenix suburban areas have lower than average buildings with more open space in the High-density Single-family Residential developments included in the study area.

**Table 18.** Displacement height  $(z_d)$  and roughness length  $(z_o)$ : Macdonald et al. (1998) equations with the average building height

Land Use Class	$z_d$ (m)	z <sub>o</sub> (m)
Residential	1.07	0.18
Low-density Single-family (< 8 units/hectare)		
High-density Single-family (≥ 8 units/hectare)	0.90	0.17
Multifamily	1.56	0.22
Mixed		
Commercial & Services	3.48	0.68
Non-high-rise		
High-rise		
Industrial	2.00	0.16
Transportation/Communications/Utilities	0	0
Mixed Industrial & Commercial		
Mixed Urban or Built-up		
Other Urban or Built-up	0.52	0.06
Predominantly Vegetated	0.52	0.06
Predominantly Built-up		
Urban High-rise		
Downtown Core Area	9.99	1.39

**Table 19.** Displacement height  $(z_d)$  and roughness length  $(z_o)$ : Macdonald et al. (1998) equations with the plan-area-weighted average building height

Land Use Class	$z_d$ (m)	z <sub>o</sub> (m)
Residential	1.17	0.19
Low-density Single-family (< 8 units/hectare)		
High-density Single-family (≥ 8 units/hectare)	0.96	0.18
Multifamily	1.75	0.25
Mixed		
Commercial & Services	5.30	1.03
Non-high-rise		
High-rise		
Industrial	2.76	0.23
Transportation/Communications/Utilities	0	0
Mixed Industrial & Commercial		
Mixed Urban or Built-up		
Other Urban or Built-up	0.80	0.09
Predominantly Vegetated	0.80	0.09
Predominantly Built-up		
Urban High-rise		
Downtown Core Area	12.23	1.71

**Table 20.** Displacement height  $(z_d)$  and roughness length  $(z_o)$  for different cities

Location	Land Use Class	$z_d$ (m)	<i>z</i> <sub>o</sub> (m)	Source
Salt Lake City, UT	Multifamily residential	9.26	2.12	Burian et al. (2002c)*
Los Angeles, CA	Multifamily residential	9.24	2.12	Burian et al. (2002b)*
Arcadia, CA	Suburban residential	6.75	1.50	Grimmond and Oke (1999), Fig. 4
Salt Lake City, UT	High-density single- family residential	5.18	1.15	Burian et al. (2002c)*
Vancouver, BC, Canada	Suburban residential	4.10	0.95	Grimmond and Oke (1999), Fig. 4
Chicago, IL	Suburban residential	4.00	0.75	Grimmond and Oke (1999), Fig. 4
Miami, FL	Suburban residential	3.25	0.80	Grimmond and Oke (1999), Fig. 4
Sacramento, CA	Suburban residential	3.10	0.75	Grimmond and Oke (1999), Fig. 4
San Gabriel, CA	Suburban residential	2.35	0.6	Grimmond and Oke (1999), Fig. 4
Los Angeles, CA	High-density single- family residential	2.24	0.44	Burian et al. (2002b)*
Tucson, AZ	Suburban residential	2.10	0.40	Grimmond and Oke (1999), Fig. 4
Phoenix, AZ	Multifamily residential	1.76	0.27	This Report*
Salt Lake City, UT	Industrial	6.10	1.27	Burian et al. (2002c)*
Los Angeles, CA	Industrial	3.04	0.54	Burian et al. (2002b)*
Phoenix, AZ	Industrial	2.35	0.29	This Report*
Vancouver, BC, Canada	Light industrial	2.25	0.5	Grimmond and Oke (1999), Fig. 4
Los Angeles, CA	Commercial & services high-rise	32.11	5.31	Burian et al. (2002b)*
Los Angeles, CA	Downtown core area	27.38	535	Burian et al. (2002b)*
Salt Lake City, UT	Downtown core area	21.54	4.78	Burian et al. (2002c)*
Vancouver, BC, Canada	Central city	20.00	4.50	Grimmond and Oke (1999), Fig. 4
Phoenix, AZ	Downtown core area	11.55	2.63	This Report*
Mexico City, Mexico	Central city	8.00	1.60	Grimmond and Oke (1999), Fig. 4

<sup>\*</sup> Phoenix, SLC, and LA values computed using the Raupach (1994) equations and the plan-area-weighted building height

## 5.0 Summary

This report summarizes the results of the derivation of building morphological characteristics for a 16.7 km<sup>2</sup> area of downtown Phoenix, Arizona. A three-dimensional building dataset and detailed land use/land cover information were integrated and analyzed using a geographic information system (GIS). Building height characteristics (e.g., mean height, height variance, height histograms) were determined for the entire study area and broken down by land use type. Parameters describing the urban morphology were also calculated including the building plan area fraction  $(\square_p)$ , building area density  $(a_P(z))$ , rooftop area density  $(a_r(z))$ , frontal area index  $(\square_l)$ , frontal area density  $(a_l(z))$ , complete aspect ratio  $(\square_l)$ , building surface area to plan area ratio  $(\square_B)$ , and the height-to-width ratio  $(\square_S)$ . These urban morphological parameters were calculated for the entire study area, for different land use types, and in some cases as a function of height above ground elevation. Using the urban morphological parameters, the aerodynamic roughness length  $(z_0)$  and displacement height  $(z_d)$  were calculated for the entire study area and for each land use type using standard morphometric equations. Most of the calculated morphometric parameters were found to be similar to values computed for other cities by other researchers. Synthesis of the results indicates that the urban morphological parameters vary significantly between different land uses. Moreover, the urban land uses containing tall buildings were found to have significantly different morphological characteristics than other urban land uses.

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# **APPENDIX 1 MAG Land Use Aggregation**

The aggregation of the MAG land use to the two classification schemes is shown below in Table A1.1. Unlike previous studies, we were unable to define the land use as High-rise and Non-high-rise because the MAG dataset did not contain this information.

Table A1.1. MAG LULC aggregation.

MAG Land Use Type	Classification Level 1	Classification Level 2	High-rise or Non-high-rise
Rural (1)	Other Urban or Built-up	Predominantly Vegetated	
Large Lot Residential (2)	Residential	Low-density Single-family Residential	
Small Lot Residential (3)	Residential	High-density Single-family Residential	
Medium Density Residential (4)	Residential	Multifamily Residential	
High Density Residential (5)	Residential	Multifamily Residential	
Neighborhood Retail Center (6)	Commercial & Services	Commercial & Services	
Community Retail Center (7)	Commercial & Services	Commercial & Services	
Regional Retail Center (8)	Commercial & Services	Commercial & Services	
Hotel, Motel or Resort (9)	Commercial & Services	Commercial & Services	
Warehouse/Distribution Center (10)	Industrial	Industrial	
Industrial (11)	Industrial	Industrial	
Business Park (12)	Commercial & Services	Commercial & Services	
Office (13)	Commercial & Services	Commercial & Services	
Educational (14)	Commercial & Services	Commercial & Services	
Institutional (15)	Commercial & Services	Commercial & Services	
Public Facility (16)	Commercial & Services	Commercial & Services	
Large Assembly Area (17)	Industrial	Industrial	
Transportation (18)	Transportation/Communications/Utilities	Transportation/Communications/Utilities	
Airport (19)	Transportation/Communications/Utilities	Transportation/Communications/Utilities	
Recreational Open Space (20)	Other Urban or Built-up	Predominantly Vegetated	
Dedicated or Non-developable Open Space (21)	Other Urban or Built-up	Predominantly Vegetated	
Water (22)	Other Urban or Built-up	Predominantly Built-up	
Agriculture (23)	Other Urban or Built-up	Predominantly Vegetated	
Vacant (24)	Other Urban or Built-up	Predominantly Vegetated	

# **Appendix 2 Description of Land Use Types**

The land use/ land cover classification we used for the building analysis was divided into two levels as shown in Table A2.1. The first level corresponds to the Anderson Level 2 classification used by the USGS for its standard national dataset. The second level includes the subdivision of the level 1 **Residential**, **Commercial and Services**, and **Other Urban or Built-up** categories. Descriptions of the level 1 and level 2 categories included on our land use classification follow Table A2.1. In addition to the multi-level classification we also categorize all the land use parcels that contain high-rise buildings as **Urban High-rise**. Finally, using aerial photographs and other information we defined the downtown city center area and termed this land use as **Downtown Core Area**. Note that **Urban High-rise** and **Downtown Core Area** contain the level 1 and level 2 land use categories, i.e., Table A2.1 will have overlap.

**Table A2.1.** Land use classification. Level 1 categories are shown in boldface, level 2 categories are indented.

# **Land Use Class** Residential Low-density Single-family ( 8 units/hectare) High-density Single-family (> 8 units/hectare) Multifamily Mixed **Commercial and Services** Non-high-rise High-rise Industrial **Transportation/Communications/Utilities Mixed Industrial and Commercial** Mixed Urban or Built-up Other Urban or Built-up Predominantly Vegetated Other Predominantly Built-Up **Urban High-rise Downtown Core Area**

#### Residential

Includes areas of single-family residences, multi-unit dwellings, mobile homes, and mixtures of residential land use types.

Low-density Single-family: Detached residential housing units with an average density less than or equal to 8 units per hectare ( 3 units/acre).

*High-density Single-family*: Detached residential housing units with an average density greater than 8 units per hectare ( $\square$  3 units/acre).

*Multifamily*: Residential housing units designed to contain multiple families in a single structure. Includes apartments and condominiums.

*Mixed*: A mixture of low-density single-family, high-density single-family, and multifamily residential land uses.

#### **Commercial and Services**

Commercial and services land use includes areas which are used predominantly for business or the sale of products and their associated services. This level 1 category is divided into non-high-rise and high-rise level 2 categories. Includes shopping malls, business districts, office buildings, strip malls, educational and institutional, and other commercial areas.

#### **Industrial**

Industrial land use includes areas where manufacturing, assembly, processing, packaging, or storage of products takes place.

## Transportation/Communication/Utilities

Areas devoted to major transportation, such as airports, freeways, roads, railways and harbor facilities. Also included are areas devoted to communications and utilities.

#### **Mixed Industrial and Commercial**

Areas included are a mixture of industrial and commercial land uses.

## Mixed Urban or Built-Up

Areas included are a mixture of the other urban land uses with none being the dominant.

# Other Urban or Built-Up

Other land use areas that cannot be categorized in the above categories. Urban vegetation and bare soil classes are categorized in this class for this scheme.

*Predominantly Vegetated*: Areas included are urban land uses that are predominantly vegetation, such as golf courses, parks, recreation fields, cemeteries, and so on. Some buildings may be contained on the site.

Other Predominantly Built-up: Includes urban land uses not categorized in any of the above land uses and that are not predominantly vegetated. These land uses are generally ambiguous or unknown.

### **Urban High-rise**

Land use that contains high-rise buildings. High-rise buildings are subjectively selected based on their relative size compared to the surrounding buildings. In general, Urban High-rise was designated for land uses containing buildings with heights in excess of 10 stories.

#### **Downtown Core Area**

Subjective designation of the downtown core area based on aerial photograph, street maps, building datasets, and other information.